

* System units

[1] international system (SI)

distance (metre)

$$\text{mile} = 1609 \text{ m}$$

force (Newton) or Kg m/sec

Power (watt) or N-m/sec

mass (Kg).

$$\text{tonne} = 1000 \text{ Kg}$$

$$\text{acceleration of gravity } g = 9.81 \text{ m/sec}^2$$

velocity m/sec or mile.p.h

* British system

distance (ft)

$$\text{inch} = 2.54 \text{ cm}$$

$$1 \text{ ft} = 12 \text{ inch}$$

$$\text{Foot} = 12 \text{ inch}$$

$$\text{mile} = 1760 \text{ yd}$$

$$= 5280 \text{ ft}$$

force (lb. wt)

power (lb. wt. ft per sec)

* mass (pound weight) (lb)

$$1 \text{ ton} = 2240 \text{ (lb.wt)}$$

* acceleration of gravity (32.2 ft/sec^2)

- velocity (ft/sec)

* torque produced by Motors:

$$T_m = T_L + T_f + J \frac{dw}{dt}$$

$T_L \Rightarrow$ عزم الحمل

T_f عزم الدوران الناتج عن الاحتكاك

$J \frac{dw}{dt}$ عزم القصور الذاتي

وهو العزم الحتمي للسكك الحديدية وقطاراتها عند التوقف

سرعة منطلقة

$$T_m = T_L + T_f$$

$$v = \omega \cdot r$$



* Types of Motors used in Electric traction

[1] dc Motors

تغير بانخفاض سرعة المحرك بوقت

ذات مدى واسع لتغير السرعة

- أما كلفة تكاليف إنتاجها للدوران

تغيرها ليزداد حركتها مناسب

[2] Induction Motors

مناسبة للتصميمات التي تحتاج لسرعة ثابتة

- Squirrel Cage rotor

- wound rotor

[3] Synchronous Motors

مناسبة للتصميمات التي تحتاج سرعة دوران ثابتة

ومدارات كبيرة، أما كلفة تصميمها عند سرعات عالية

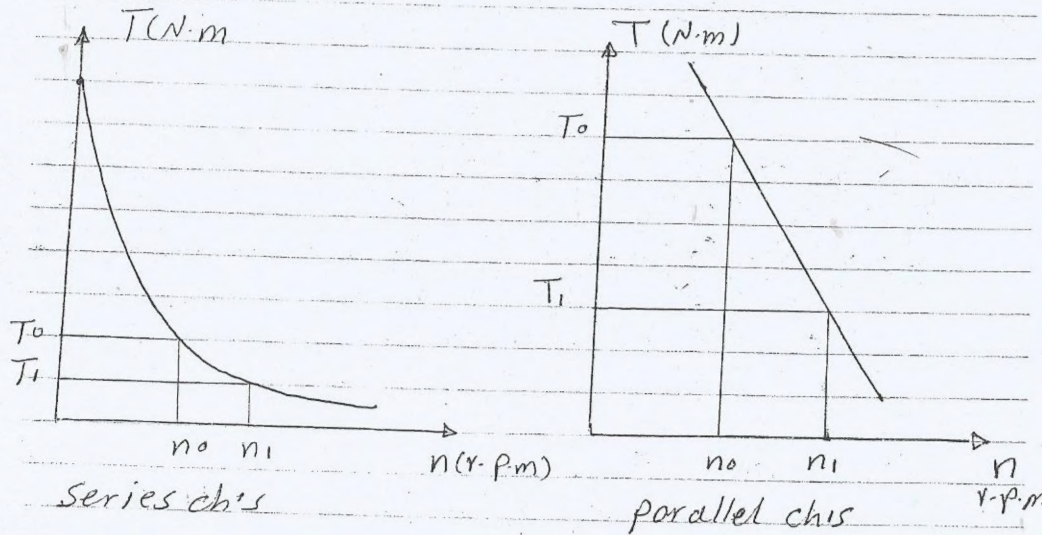
منخفضة، كلفة تشغيل مرتفعة

* General ch's of Electric traction Motors:

a) High starting torque

للطلب على الطاقة ولا يحد على إحصاء مع المطلوب

b) Series ch's between torque and speed



1- إذا كانه حثالة محركه متناقصه فكلما نظرنا إلى حثالاته نجد أنه صغر من
سرعته أي كلما صغر الحثالة كلما صغر السرعة n_0, n_1

2- إذا كانه محركه لها خاصية لتوازي في أنه لها قوة من الحثالة كبيرة
فكلما صغر الحثالة كلما صغر السرعة أي كلما صغر الحثالة كلما صغر السرعة
con fairly

3- إذا كانه محركه لها خاصية لتوازي في أنه لها قوة من الحثالة كبيرة
فكلما صغر الحثالة كلما صغر السرعة أي كلما صغر الحثالة كلما صغر السرعة
Series الحثالة لا تتغير مع السرعة أي كلما صغر الحثالة كلما صغر السرعة
 $T \propto 1/n$

(c) easy to control in speed

d) Has ability to using electric breaking.

e) " " " standing suddenly change in voltage

(f) " " " standing cutting off source of supply
تجدد الانقطاع إلى وقت لاحق
أي أنه كلما صغر الحثالة كلما صغر السرعة
سرعته كلما صغر الحثالة كلما صغر السرعة

(g) hardness, weight and volume
يجب أن تكون وزنها صغيرة في قدر الحثالة لا تتغير مع السرعة
وذلك في حثالة صغيرة وحقبة الحثالة لا تتغير مع السرعة

* System of electric traction

can be divided according to getting their power to main groups.

(a) Vehicles generate its own Energy and subdivided according to the nature of generation or storage

- diesel ~~engine~~ electric train or ships
- petrol electric trucks, lorries
- the battery-driven road vehicles

(b) Vehicles receive their power from distributing network fed by a few large generating stations

- dc station } tramways rail ways
- ac station } trolley buses

* Types of Power supply used in electric traction.

(a) dc Current system

600 - 700v (tram)
 1500 - 3000v (trolley)

(b) Single phase system

11-15 Kv with $f = 16 \frac{2}{3}$ (Hz) or 25 Hz

300-400 volts
 11-15 Kv
 16 2/3 Hz or 25 Hz

(c) Three phase system

3.3 Kv $f = 16 \frac{2}{3}$ Hz

Three phase system
 3.3 Kv
 16 2/3 Hz



* Advantages of Electric traction.

- 1- it is a cleanliness so it essential for use in underground and tube railways
- 2- rapid & smooth acceleration and braking
- 3- Have a large speed than steam traction electric traction \rightarrow 1-20 Mph
steam \rightarrow 0.4-0.5 Mph
- 4- easy to stop specially in frequent stops
- 5- need less time for maintenance and repair
So less cost to maintenance and repair by 50%
- 6- Can carry more people than steam traction because of higher average speed.
- 7- it can be used immediately at any time it connected to supply so better utilization
- 8- No smoke or sparks and no damage to building due to smoke fumes so it is safety
- 9- Saving in cost and energy due to absence of cooling and water depots (خارج) and also time of cooling of engines.

10. the electric braking method is better than mechanical braking due to

- less wear on brake shoes
- less heat wasted in the brake shoes

* Disadvantages of E.T.

1. High cost required to convert from steam to electric traction due to overhead equipment and feeders.
2. Failure in power supply for a few minutes may cause cut off services for hours so increase reliability of supply.
3. Formation of ice layers on conductor rails will prevent the train to get its power, this can be overcome by running a service locomotive up and down the line to prevent ice formation.
4. the interference between the power line with telephone and telegraph lines runs along the track so high cost for moving lines away the tracks or replaced by cable.
5. require a power for heating the compartments at high cost.



* Mechanics of train movement.

$$T = F' \times \frac{P}{2}$$

$$F' = \frac{2T}{P}$$

gear efficiency

$$\eta = \frac{F D / 2}{F' d / 2}$$

$$\eta = \frac{F}{2T} \left(\frac{P}{d} \right) D$$

$$G = d/P \text{ gear ratio}$$

$$\eta = \frac{F}{2T G} \frac{1}{D} \Rightarrow F = \eta \frac{2T G}{D}$$

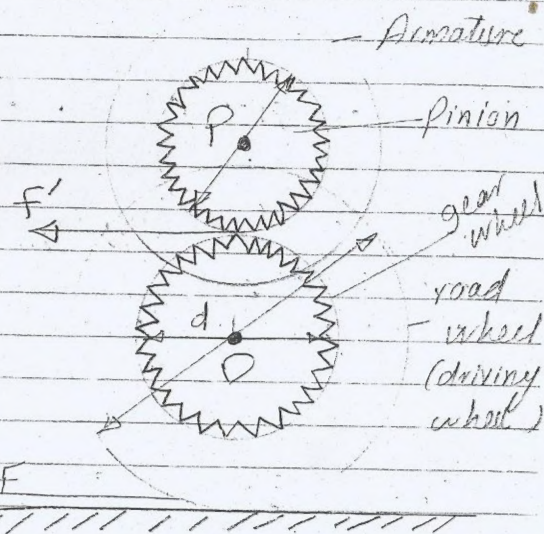
$$F = \eta T \times \left(\frac{2G}{D} \right) \quad \#$$

tractive effort on driving wheel

tractive effort on driving wheel (1) \Rightarrow tractive effort $= F'$

gear wheel (d)

(ad & coefficient of adhesion) = $\frac{\text{tractive effort to slip the wheel}}{\text{adhesive weight}}$



| | | | | | | |
|-------------|------|------|------|------|------|------|
| Speed m.p.h | 0 | 10 | 20 | 30 | 40 | 50 |
| μ_{ad} | 0.25 | 0.16 | 0.14 | 0.12 | 0.10 | 0.09 |

if rails are greasy (oil) the value is 0.08

Ex) if train has weight m (tons) and third of weight is driving wheel
what the max acceleration of μ_{ad} 0.25

Solution.

$$\mu_{ad} = F/w \quad F = \mu_{ad} w$$

$$m \cdot a = \mu_{ad} m \cdot g$$

$$a = \mu_{ad} \cdot g$$

$$= 0.25 \times 32.2 = 8.1 \text{ Ft/sec/sec}$$

$$= 8.1 \times \frac{0.3 \times 0.62 \times 3600}{1000} \text{ mile/h/sec}$$

$$a = 5.5 \text{ m.p.h.p.s.}$$

max acceleration

$$a = 5.5 \times 1/3 = 1.83 \text{ m.p.h.p.s.}$$

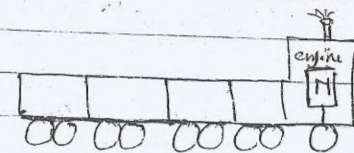
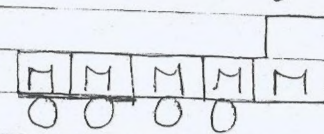


For steam traction the adhesive weight less than 50%.

$$\mu_{ad} (\text{electric traction}) > \mu_{ad} (\text{steam traction})$$

this is because:

- 1- the torque in electric traction is continuous while in steam traction is pulsating.
- 2- in E.T the driven wheels are distributed along the length of train while in steam traction they are close together.



* Tractive effort required to move the train

$$F_t = F_a + F_r + F_g$$

F_a the required T.Eff for Linear acceleration
لقدوة التسارع الخطي

F_r the required T.Eff to overcome the train resistance
للتغلب على قوة المقاومة للحركة

F_g the required T.Eff to overcome the acceleration of gravity +
توزل

* Fa calculation

if a force (Fa) (lb.wt) acts on a mass of w (tons)
the acceleration is (a)..

$$a = \frac{F_a}{m} = \frac{F_a}{(w/g)} = \frac{F_a (32.2)}{2240 w} \quad \begin{matrix} \text{ft/sec/sec} \\ \downarrow 3200 \\ 5280 \end{matrix}$$

$$a = \frac{F_a}{w} (0.01437) * \frac{0.3 * 0.62 * 3600}{1000} \quad \text{m.p.h.p.s}$$

$$F_a = 102 w a$$

lb.wt tons m.p.h.p.s

when train accelerates K.E is produced in 2 ways

① Linear motion of the train

② rotation of wheel and motors.

$$K.E_t = K.E_{\text{Linear}} + K.E_{\text{rotation}}$$

$$= \frac{1}{2} w v^2 + \sum \frac{I}{2} \omega^2, \quad \omega = v/r$$

$$= \frac{1}{2} w v^2 + \frac{I}{2} \left(\frac{v}{r} \right)^2$$

$$= \frac{1}{2} w v^2 + \frac{1}{2} v^2 \left(\frac{I}{r^2} \right) \rightarrow m \text{ (rotating mass)}$$

$$= \frac{1}{2} w v^2 + \frac{1}{2} M v^2$$



$$K.E = \frac{1}{2} (w+m) v^2$$

$$K.E = \frac{1}{2} w_e v^2$$

where

w = dead weight

w_e = effective weight or accelerating mass of the train

I = moment of inertia of rotating parts

m = 8 to 15 % of w

* tractive effort to overcome the train resistance.

$$F_r = w \cdot r \quad (\text{lb.wt})$$

r = specific train resistance (lb.wt/ton)

لحساب الجهد المبذول لتمرير القطار وتغلب على مقاومة القطار

① الجهد المبذول لتمرير القطار من المحركات (تحت تأثير الجاذبية)

② الجهد المبذول لتمرير القطار من المحركات (تحت تأثير الاحتكاك)

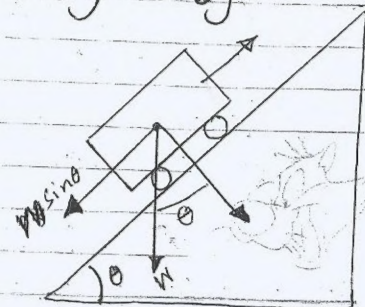
* tractive effort to overcome the gravity

$$F_g = \pm w \sin \theta$$

~~التي تكون موجبة إذا كان القطار يتحرك صاعداً~~

if G₁ = الجهد المبذول لتمرير القطار

$$G_1 = \frac{w}{\sin \theta}$$



$$G\% = \frac{y}{x} \times 100 = G'$$

$$G\% = 100 \sin \theta = G'$$

$$\sin \theta = \frac{G'}{100}$$

$$F_g = \pm w \times \frac{G'}{100} \quad \text{tons}$$

$$F_g = \pm w \frac{G'}{100} \times 2240 \rightarrow \text{Ib}$$

$$F_g = \pm 22.4 w G' \quad \text{tons} \quad (\text{Ib} \cdot \text{wt})$$

$$F_t = 102 w_{ea} + w_r \pm 22.4 w G' \quad (\text{Ib} \cdot \text{wt})$$

tons m.p.h ton Ib.wt/ton ton $\frac{y}{x} \times 100$

the output power of the driving axes

$$P = F_t v \quad \text{Ib} \cdot \text{wt} \cdot \text{ft/sec}$$

if v in (m.p.h.)

$$P = F_t \times v \left(\frac{5280}{3600} \right) \quad \text{Ib} \cdot \text{wt} \cdot \text{ft/sec}$$

$$1 \text{ h.p.} = 550 \text{ Ib} \cdot \text{wt} \cdot \text{ft/sec}$$

$$P = f_t \cdot v \left(\frac{5280}{3600 \times 550} \right) \quad (\text{h.p.})$$

$$1 \text{ h.p.} = 746 \text{ w}$$

$$P = f_t \times v \left(\frac{5280 \times 746}{3600 \times 550 \times 1000} \right) \quad (\text{Kw})$$

$$P = 0.002 f_t \cdot v \quad \text{Kw}$$

Ib.wt m.p.h

in (SI) system,

$$F_a = m_e \cdot a \Rightarrow \text{Newton}$$

$$\Rightarrow m_e \rightarrow \text{Kg} \quad a \rightarrow \text{m/sec}^2$$

$$F_a = m_e (1000) \times a \left(\frac{3000}{3600} \right)$$

$$F_a = 277.8 m_e \cdot a \quad \text{Newton}$$

Km/h/sec tonne

$$F_r = m (\text{tonne}) \times r (\text{Newton/tonne}) = m \cdot r \quad (\text{Newton})$$

$$F_g = \pm m g \sin \theta = 1000 \times 9.81 \frac{\text{m}}{\text{sec}^2} = 98.1 m \cdot c$$

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Date: _____ no: _____

$$F_t = 277.8 m \cdot a + m \cdot r + 98.1 m \cdot c \quad (N)$$

(tonne) km/h/s Newton/tonne tonne

* the required power:

if v in (m/sec)

$$P_o = F_t \cdot v \quad (\text{watt})$$

if v in (km/h)

$$P_o = F_t \cdot v \left(\frac{1000}{3600} \right) \quad (\text{watt})$$

$$= F_t \cdot v \left(\frac{1000}{3600 \times 1000} \right) \quad (\text{Kw})$$

$$P_o = \frac{F_t \cdot v}{3600} \quad (\text{Kw})$$

Newton km/h

Ex:- a motor coach train weighing 200 tons is accelerated up a gradient of 1 in 200 at a mean acceleration of 1.2 m.p.h.p.s up to speed of 30 m.p.h. find

- (1) tractive effort required
- (2) the output at the end of the accelerating period the train resistance is 10 lb/ton and $w_e = 10\%$

Solution.

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Date: _____ no: _____

$$a = 1.2 \text{ m.p.h.p.s}, W = 200 \text{ ton}, w_e = \frac{200 + 10}{100} \times 200$$

$$w_e = 220 \text{ tons}, r = 10 \text{ lb/ton}$$

$$G = \frac{1}{200} \times 100 = 0.5$$

$$F_t = 102 W \cdot a + W \cdot r + 22.4 W \cdot G$$

$$= 102 \times 220 \times 1.2 + 200 \times 10 + 22.4 \times 200 \times 0.5$$

$$F_t = 31168 \text{ (lb.wt)}$$

(2) at the end of acceleration $v = 30$ the power required

$$P_o = 0.002 F_t \cdot v \quad (\text{Kw})$$

$$= 0.002 \times 31168 \times 30$$

$$P_o = 1860 \text{ Kw}$$

Q1 train weight 240 tonnes, accelerated up gradient 1:250 of a mean acceleration 2 km/hour/sec, until the velocity reach to 60 km/h find

- ① Tractive effort
- ② the power required if $r = 50 \text{ N/t}$ & $w_e = 1.1 W$

Solution

- 18 -

Date: _____

no: _____

$$a = 2 \text{ km/h/sec}, m = 240 \text{ tonne}$$

$$m_e = 1.1 \times 240 = 264 \text{ tonne}$$

$$r = 50 \text{ N/t}, C = \frac{1}{250} \times 100 = 0.4\%$$

$$F_t = 277.8 m_e \cdot a + m \cdot r + 98.1 m \cdot C$$

$$= 277.8 \times 264 \times 2 + 240 \times 50 + 98.1 \times 240 \times 0.4$$

$$= 168096 \text{ (N)}$$

$$P_o = \frac{F_t \cdot v}{3600} = \frac{168096 \times 60}{3600} = 2802 \text{ Kw}$$

2



20X

- 19 -

Date: _____

no: _____

A train has weighing 250 tonne, run with 4 Motors accelerate up gradient 1:80 and take 20 sec to reach 42 km/sec if Gear ratio 3.5 and $\eta = 92\%$ $r = 40 \text{ N/t}$, and $W_e = 1.1 W$, $D = 92 \text{ cm}$
 * Find the torque produced by each motor

Solution.

$$a = \frac{v}{t} = \frac{42}{20} = 2.1 \text{ km/h/sec}$$

$$m_e = 1.1 \times 250 = 275 \text{ tonne}$$

$$C = \frac{1}{80} \times 100 = 1.25\%$$

$$F_t = 277.8 m_e \cdot a + m \cdot r + 98.1 m \cdot C$$

$$F_t = 277.8 \times 275 \times 2.1 + 250 \times 40 + 98.1 \times 250 \times 1.25$$

$$= 201054.5 \text{ N}$$

$$F_t = 2 \frac{G}{D} T_m$$

$$201054.5 = 2 \times 0.92 \times \frac{3.5}{0.92} \times T_m$$

$$T_m = \frac{201054.5 \times 0.92}{2 \times 0.92 \times 3.5} = 28722 \text{ N.m}$$

$$\text{Torque/Motor} = \frac{28722}{4} = 7180 \text{ N.m.}$$



* train weight 250 tonne move with 4 Motors each
 produce torque equal 8000 N.m, up gradient 3‰
 if gear ratio 3.5 and $\eta = 90\%$, $i = 50 \text{ N/t}$
 $w_e = 1.1w$ and $D = 90 \text{ cm}$ find \Rightarrow
 time required to reach 80 km/h
 if $V = 3000 \text{ volt}$, $\eta = 85\%$ for motor find the current

Solution

$$F_t = \frac{2 \eta G T_m}{D}$$

$$= \frac{2 \times 0.9 \times 3.5 \times 4 \times 8000}{0.9} = 224000 \text{ N}$$

$$C = \frac{30}{1000} \times 100 = 3\%$$

$$F_t = F_a + F_R + f_g \Rightarrow$$

$$224000 = F_a + 250 \times 50 + 98.1 \times 250 \times 3$$

$$= F_a + 86075$$

$$F_a = 137925 \text{ (N)}$$

$$F_a = 277.8 m_e a = 137925$$

$$a = \frac{137925}{277.8 m_e} = \frac{137925}{277.8 \times 1.1 \times 250} = 1.8 \text{ km/h/sec}$$



$$t = \frac{V}{a} = \frac{80}{1.8} = 44.44 \text{ sec}$$

$$\eta = \frac{P_o}{P_{in}} \Rightarrow P_{in} = \frac{P_o}{\eta}$$

$$P = F_t \cdot V \quad \text{km/h (Kw)}$$

$$\eta \times 3600$$

$$= \frac{224000 \times 80}{0.85 \times 3600} = 5856 \text{ Kw}$$

$$\text{total Current} = \frac{5856000}{3000} = 1952 \text{ (A)}$$

$$\text{Current / Motor} = 1952 / 4 = 488 \text{ (A)}$$

* Types of Service for people carrying with E.T.

أنواع خدمات نقل الركاب بالترامواي

● City Service

خدمات المدينة

حيث تكون المسافة المغطاة متوسطة تقريباً كل 1 كيلومتر ووسط

البنية التحتية وخدمات النقل

● Suburban city service

خدمات المدينة

حيث تكون المسافة المغطاة 2-4 كيلومتر والمسافة بين المحطات 30-40 كم

● main line service

خدمات المدينة

حيث تكون المسافة المغطاة طويلة جداً وخدمات النقل

والبنية التحتية وخدمات النقل



* Speed time Curves:

there are 2 curves:

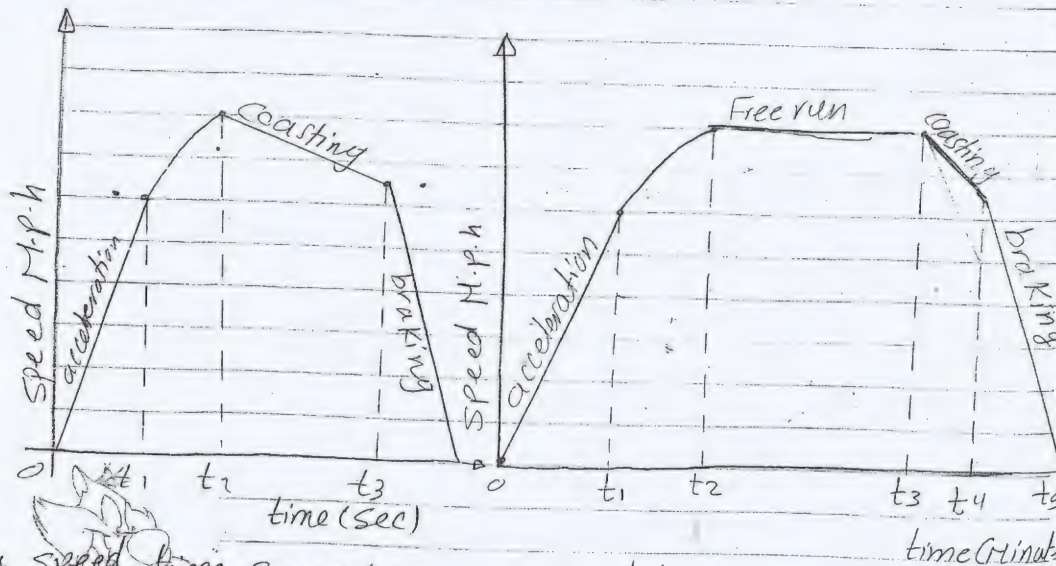
[1] Speed time curve

(النمط)

[2] distance-speed curve

the importance of speed-time curve when we study the motion of train is:

- 1- لأن قراءة السرعة مباشرة عن أي كلف زمنية
- 2- ميل لها من يبين استهلاك الطاقة والوقت
- 3- كما أنه يوضح مدى كفاءة العمل



* Speed-time Curve in City service.

* Speed-time curve in main line service

1- فترة التسارع (0-t₁) : يبين الحد الأقصى للسرعة التي يمكن أن تصل إليها القاطنة

على القاطنة

2- فترة السرعة (t₁-t₂) : هي الفترة التي تقضيها القاطنة في السرعة

التي يجب أن تكون متساوية للفترة التي تقضيها القاطنة في التسارع

تأخير (t₂)

3- فترة الانطلاق (t₂-t₃) : بعد انقضاء سرعة القاطنة

بالفترة التي طولها يساوي سرعة القاطنة

4- فترة التوقف (t₃-t₄) : يتم فصل القاطنة عن مصدر الطاقة في هذه الفترة

فصل القاطنة عن مصدر الطاقة في هذه الفترة

1- سرعة القاطنة في هذه الفترة هي سرعة القاطنة في التسارع

السرعة التي تستخدمها القاطنة في التسارع

بدل من التسارع في التسارع

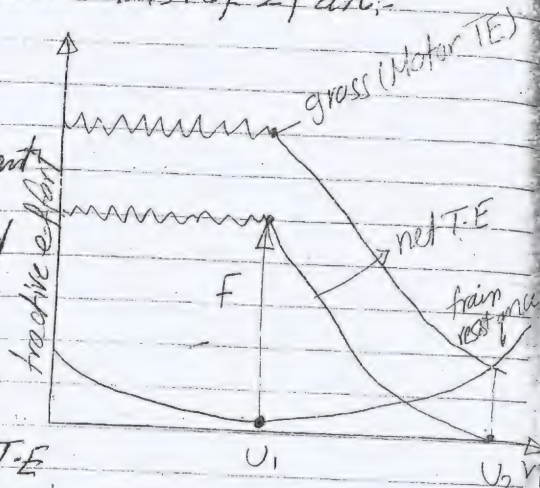
5- فترة التوقف (t₄-t₅) : فترة التوقف التي تستغرقها القاطنة في التوقف

أو التوقف في التوقف

* The acceleration period consist of 2 part:

[1] the first part:

- the motor T.E kept constant this occurs until all the resistance are switched out at speed (U_1)
 - the tractive effort available for acceleration is (F) and it is the different between motor T.E and train resistance
 - the acceleration is this period is nearly constant



[2] the second part:

- the tractive effort falls rapidly with speed and train resistance increase slowly and then rapidly until (U_2) where motor T.E = train resistance so the net tractive effort available for acceleration is zero

$U_2 \Rightarrow$ max possible speed.

① Crest speed: max speed attained on the Run

② average speed: the mean speed from start to stop



$$V = \frac{S}{T} = \text{mile}$$

per hour
 في الساعة

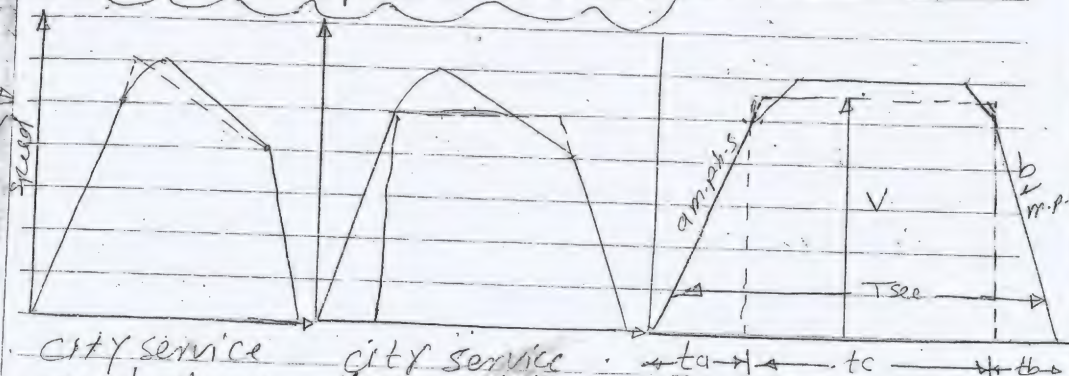
③ Schedule speed: mean speed when stop periods are included

$$V = \frac{S}{T + T_{stop}}$$

السرعة
 في الساعة

main line has crest speed 56 m.p.h

* Simplified speed time curves:



city service
 quadrilateral

city service
 trapezoidal

main line service

- speed time curve for city service can be replaced by quadrilateral or trapezoidal fig

- the main line service speed time curve replaced by trapezoidal fig.

* for main line service prove that

$$V = \frac{1}{2K} \left[T - \sqrt{T^2 - 14400SK} \right]$$

where

$$K = \frac{1}{2a} + \frac{1}{2b}$$

a: uniform acceleration in m.p.h.p.s

b: uniform braking in m.p.h.p.s

V: crest speed in m.p.h

S: distance to run in (mile)

T: time in sec

* Prove *

duration of acceleration (t_a) = V/a

" " braking (t_b) = V/b

distance of acc = $\frac{1}{2} V t_a = \frac{1}{2} \frac{V^2}{a}$

" " braking = $\frac{1}{2} V t_b = \frac{1}{2} \frac{V^2}{b}$

distance of free run or coasting = $V T_c$

$$= V (T - t_a - t_b) = (T - \frac{V}{a} - \frac{V}{b}) V$$



$$= V T - \frac{V^2}{b} - \frac{V^2}{a}$$

$$\text{total distance} = \frac{V^2}{2b} + \frac{V^2}{2a} + V T - \frac{V^2}{a} - \frac{V^2}{b}$$

$$S' = V T - V^2 \left(\frac{1}{2a} + \frac{1}{2b} \right) \frac{\text{mile}}{3600} \times 3600$$

a, b in m.p.h.p.s, V = m.p.h, T in sec

$$S' = \frac{\text{mile} \times \text{sec}}{\text{hr} \times 60 \times 60} \text{ hours distance}$$

$$S' = \frac{\text{mile} \times \text{sec}}{3600 \text{ sec}} \Rightarrow \text{miles}$$

if we want the distance in miles (S say)

$$\frac{S'}{3600} = S \text{ or } S' = 3600 S$$

$$3600 S = V T - V^2 \left(\frac{1}{2a} + \frac{1}{2b} \right)$$

$$3600 S = V T - K V^2$$

$$K V^2 - V T + 3600 S = 0$$

$$V = \frac{T \pm \sqrt{T^2 - 4 \times 3600 S K}}{2K}$$

$$\text{m.p.h} \rightarrow V = \frac{1}{2K} \left(T \pm \sqrt{T^2 - 14400 S K} \right) \frac{\text{mile}}{\text{hr}}$$

$$T_c = T - t_a - t_b = T - \frac{V}{a} - \frac{V}{b} = T - V \left(\frac{1}{a} + \frac{1}{b} \right)$$

$$T_c = T - 2 K V$$

3600 is 1 hour in sec
mile = 3600 ft
S' = 3600 S
S = S' / 3600
mile

$$2KV = T \pm \sqrt{T^2 - 14400K}$$

$$T_c = T - (T \pm \sqrt{T^2 - 14400K})$$

$$T_c = \mp \sqrt{T^2 - 14400K}$$

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$$T_c = T - 2KV = \mp \sqrt{T^2 - 14400K}$$

±

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$$2KV = T \pm \sqrt{T^2 - 14400K}$$

$$V = \frac{1}{2K} \left[T \pm \sqrt{T^2 - 14400K} \right]$$



Ex1 $V = 38$ m.p.h, maximum running speed
the average distance between stops is 2200 yd
the schedule speed in standing a station stop of
20 sec is 25 m.p.h find the necessary acceleration
allowing a maximum retardation of 2.5 m.p.h.ps

$$S = 2200 \text{ yd} = 1.25 \text{ miles}$$

$$V_{sh} = 25 \text{ m.p.h} \quad t_{stop} = 20 \text{ sec}$$

$$\text{time of travel include stop time} = \frac{S}{V} = \frac{1.25}{25} = 0.05 \text{ hr}$$

$$T = 3 \text{ minute} = 180 \text{ sec}$$

$$\text{time of travel} = T - T_{stop} = 180 - 20 = 160 \text{ sec}$$

$$KV^2 - VT + 3600S = 0$$

$$K = \frac{VT - 3600S}{V^2} = \frac{1}{2a} + \frac{1}{2b}$$

$$\frac{1}{a} = \frac{2}{V^2} \left(VT - 3600S - \frac{1}{b} \right)$$

Handwritten note: $\frac{1}{b} = \frac{1}{20}$

$$\frac{1}{a} = \frac{2}{38^2} \left(38 \times 160 - 3600 \times 1.25 - \frac{1}{20} \right)$$

$$\frac{1}{a} = 1.76 \Rightarrow a = 0.57 \text{ m.p.h.ps}$$

* Sheet

1 Two stops per mile \Rightarrow Distance $S = 0.5$ mile

Schedule speed 17 [m.p.h]

Time of stop $t_s = 20$ [sec]

acceleration $= 1.2$ [m.p.h.p.s]

braking retardation $b = 2$ [m.p.h.p.s]

* Determine the trapezoidal speed time curve?

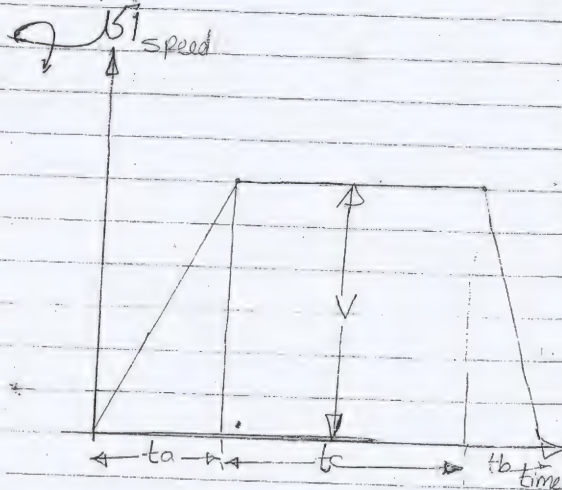
$$V_{\text{schedule}} = \frac{S}{T + t_s}$$

$$17 = \frac{0.5}{T + 20}$$

$$T + 20 = 0.0294 \text{ hr}$$

$$T + 20 = 105.88 \text{ Sec}$$

$$T = 85.88 \text{ Sec}$$



$$V = \frac{1}{2K} \left[T - \sqrt{T^2 - 14400SK} \right]$$

$$K = \frac{1}{2a} + \frac{1}{2b} = \frac{1}{2 \times 1.2} + \frac{1}{2 \times 2} = 0.66$$

ROX

$$V = \frac{1}{1.33} \left[85.88 - \sqrt{(85.88)^2 - 14400 \times 0.5 \times 0.66} \right]$$

$$V = 26.06 \text{ [m.p.h]}$$

$$t_a = \frac{V}{a} = \frac{26.06}{1.2} = 21.7 \text{ [sec]}$$

$$t_b = \frac{V}{b} = \frac{26.06}{2} = 13 \text{ [sec]}$$

$$t_c = T - t_b - t_a = 51 \text{ [sec]}$$

2 distance between stops = 1 mile

Schedule speed = 25 [m.p.h]

Time of stop (t_s) = 20 [sec]

braking retardation = 2.25 [m.p.h.p.s]

max speed = 1.25

average speed

* Assuming a trapezoidal speed time curve and calculate the acceleration.

$$V_{\text{sch}} = 25 \text{ m.p.h}$$

$$25 = \frac{S}{T + t_s}$$

$$T + 20 = \frac{1}{25} = 0.04 \text{ [hr]}, T = 124 \text{ [sec]}$$

$$V_{av} = \frac{\text{Distance of Run}}{\text{time of Run}} = \frac{1}{124} = 0.00806 \text{ m.p.s}$$

$$V_{av} = 29.03 \text{ m.p.h}$$

$$\frac{V_{max}}{V_{av}} = 1.25 \Rightarrow V_{max} = 1.25 \times V_{av}$$

$$V_{max} = 1.25 \times 29.03 = 36.3 \text{ m.p.h}$$

$$V_{max} = \frac{1}{2K} \left[T - \sqrt{T^2 - 14400SK} \right]$$

$$36.3 = \frac{1}{2K} \left[124 - \sqrt{(124)^2 - 14400 \times 1 \times K} \right]$$

$$72.6K = 124 - \sqrt{15376 - 14400K}$$

$$(72.6K - 124)^2 = (-\sqrt{15376 - 14400K})^2$$

$$(72.6K)^2 - 2 \times 72.6 \times 124K + 124^2 = 15376 - 14400K$$

$$5270.76K^2 - 18004.8K + 15376 = 15376 - 14400K$$

$$5270.76K^2 - 3604.8K = 0$$

$$K = \frac{3604.8}{5270.76} = 0.683$$

$$\frac{1}{2a} + \frac{1}{2b} = \frac{1}{2a} + \frac{1}{2 \times 2.25} \quad 0.22$$

$$\frac{1}{2a} = K - 0.222 = 0.461$$

$$2a = 2.169 \Rightarrow a = 1.08 \text{ [m.p.h.p.s]}$$

3 $U_1 = 25 \text{ m.p.h}$, $t_a = 20 \text{ sec}$, $t_c = 40 \text{ sec}$
 $T = 70 \text{ sec}$ (city service)

$$b_c = 0.1 \text{ [m.p.h.s]}$$

Determine the distance run from start to stop and the average speed. (Trapezoidal)
 (quadrilateral)

$$T = t_a + t_b + t_c = 70 \text{ sec}$$

$$t_b = T - t_a - t_c = 70 - 20 - 40 = 10 \text{ sec}$$

$S_T =$ total distance of the Run

$$= S_a + S_b + S_c$$

$$= \frac{1}{2} t_a U_1 + \frac{1}{2} t_b V_2 + \frac{1}{2} t_c (V_2 + V_1)$$

$$U_2 = U_1 - b_c t_c \quad \# \quad b_c = \frac{V_1 - V_2}{t_c} \Rightarrow V_1 - V_2 =$$

$$U_2 = 25 - 40 \times 0.1$$

$$U_2 = 21 \text{ m.p.h}$$

$$\text{Slope} = b_c = \frac{U_1 - U_2}{t_c}$$

$$U_2 = U_1 - b_c t_c$$

$$S_T = \frac{1}{2} \times \frac{20}{3600} \times 25 + \frac{1}{2} \times \frac{10}{3600} \times 21 + \frac{1}{2} \times \frac{40}{3600} (25 + 21)$$

$$S_T = 0.354 \text{ mile}$$

$$V_{av} = \frac{S_T}{T} = \frac{0.354}{70 \text{ sec}} = 18.2 \text{ m.p.h}$$

41 $S = 1.2 \text{ miles}$, $V_{sch} = 25 \text{ m.p.h.}$, $t_s = 20 \text{ sec}$
 Coasting retardation $= 0.1 \text{ m.p.h.s}$
 Braking retardation $= 2 \text{ m.p.h.s}$

$$V_1 = 38 \text{ m.p.h.} = U_{max}$$

assume quadrilateral speed-time curve and Determine

a) the acceleration

b) duration of coasting period

$$V_{sch} = \frac{S}{T+t_s} = 25$$

$$T+20 = \frac{1.2}{25} = 0.048 \text{ hr}$$

$$20 + T = 172.8 \text{ [sec]}$$

$$T = 152.8 \text{ sec}$$

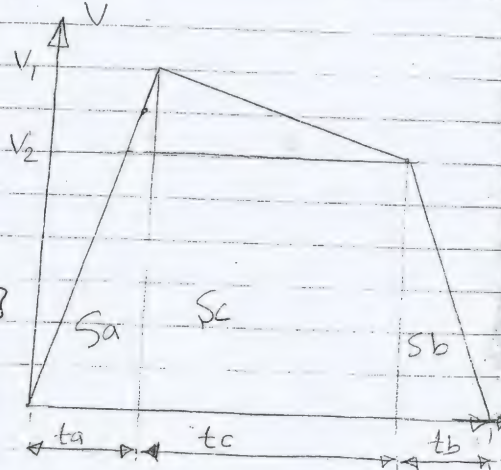
$$\tan \theta = 0.1 = \frac{U_1 - U_2}{t_c}$$

$$S_T = S_a + S_b + S_c$$

$$= \frac{1}{2} t_a U_1 + \frac{1}{2} t_b U_2 + \frac{1}{2} t_c (U_1 + U_2)$$

$$\text{but } t_a = \frac{U_1}{a}, t_b = \frac{U_2}{b}, t_c = T - t_a - t_b$$

$$U_2 = U_1 - 0.1 t_c \quad \#$$



$$U_2 = b t_b$$

$$2 t_b = U_1 - 0.1 t_c \quad (U_1 = 38 \text{ [m.p.h.]})$$

$$t_b = 19 - 0.05 t_c$$

$$T = t_a + t_b + t_c$$

$$t_a = T - t_b - t_c$$

$$= 152.8 - 19 + 0.05 t_c - t_c$$

$$t_a = 133.9 - 0.95 t_c$$

$$S_T = \left[\frac{1}{2} (133.9 - 0.95 t_c) \times 38 + \frac{1}{2} (19 - 0.05 t_c) (38 - 0.1 t_c) + 0.5 t_c (76 - 0.1 t_c) \right]$$

$$= \frac{1}{7200} [5810.2 + 36.1 t_c - 0.045 t_c^2]$$

$$8640 = 0.045 t_c^2 + 36.1 t_c - 5810.2$$

$$t_c^2 - 380 t_c + 29787.4 = 0$$

$$t_c = \frac{380 \pm \sqrt{(380)^2 - 4 \times 29787.4}}{2 \times 1}$$

$$t_c = 190 \pm 79.75$$

$$t_c = 269.45 \text{ or } 110.55 \text{ sec}$$

$$\text{at } t_c = 110.55 \text{ sec}$$

$$t_a = 133.9 - (0.95 \times 111) = 28.45 \text{ [sec]}$$

$$V_2 = 38 - (0.1 \times 111) = 26.4 \text{ [m.p.h]}$$

$$a = \frac{V_1}{t_a} = \frac{38}{28.45} = 1.335 \text{ [m.p.h.p.s]}$$

5 $S = 1 \text{ miles}$, $V_{avg} = 25 \text{ m.p.h}$, $a = 1.25 \text{ m.p.h.s}$

Coasting retardation = 0.1 m.p.h.p.s

Braking retardation = 2 m.p.h.p.s

assume Quadrilateral speed time curve and Determine.

- 1) the duration of acceleration period
- 2) " " " " Coasting "
- 3) " " " " Braking "
- 4) distance run during these periods.

$$V_{avg} = \frac{ST}{T} = 25 \text{ [m.p.h]}$$

$$T = \frac{1}{25} = 0.04 \text{ [hr]}$$

$$T = 144 \text{ [sec]}$$

$$U_2 = U_1 - t_c bc$$

$$U_2 = U_1 - (T - t_a - t_b) bc$$

$$t_a = \frac{U_1}{a}, t_b = \frac{U_2}{b}$$

$$U_2 = U_1 - (T - \frac{U_1}{a} - \frac{U_2}{b}) bc$$

$$U_2 = U_1 - (T bc - \frac{U_1}{a} bc - \frac{U_2}{b} bc)$$

$$U_2 = U_1 - T bc + \frac{U_1}{a} bc + \frac{U_2}{b} bc$$

$$U_2 (1 - \frac{bc}{b}) = U_1 (1 + \frac{bc}{a}) - T bc$$

$$U_2 (1 - \frac{0.1}{2}) = U_1 (1 + \frac{0.1}{1.25}) - (144 \times 0.1)$$

$$0.95 U_2 = 1.08 U_1 - 14.4$$

$$U_2 = 1.137 U_1 - 15.2$$

$$S_T = S_a + S_b + S_c$$

$$= \frac{1}{2} [t_a U_1 + t_c (U_1 + U_2) + t_b U_2]$$

$$1 = \frac{1}{7200} \left[\frac{U_1^2}{a} + (U_1 + U_2) (T - \frac{U_1}{a} - \frac{U_2}{b}) + \frac{U_2^2}{b} \right]$$

$$7200 = \frac{U_1^2}{a} + U_1 T - \frac{U_1^2}{a} - \frac{U_1 U_2}{b} + U_2 T - \frac{U_1 U_2}{a} - \frac{U_2^2}{b} + \frac{U_2^2}{b}$$

$$= U_1 T + U_2 T - U_1 U_2 (\frac{1}{a} + \frac{1}{b})$$

$$= 144 U_1 + 144 (1.137 U_1 - 15.2) - U_1 \times 1.3 \times (1.137 U_1 - 15.2)$$

$$= 144 U_1 + 163.7 U_1 - 2188.8 - 1.48 U_1^2 + 19.76 U_1$$

$$7200 = 327.5 U_1 - 2188.8 - 1.98 U_1^2$$

$$0 = 327.5 U_1 - 9388.8 - 1.98 U_1^2$$

$$U_1^2 - 221.3 U_1 + 634.0 = 0$$

$$U_1 = \frac{221.3 \pm \sqrt{(221.3)^2 - 4 \times 6343.8}}{2}$$

$$U_1 = \frac{221.3 \pm 153.6}{2}$$

$$U_1 = 110.65 \pm 76.8$$

$$U_1 = 188 \text{ [mph]} \text{ or } (U_1 = 33.85) \text{ [mph]}$$

$$U_2 = (1.137 \times 33.85) - 15.2$$

$$(U_2 = 23.3) \text{ [mph]}$$

$$t_a = \frac{U_1}{a} = \frac{33.85}{1.25} = 27 \text{ [sec]}$$

$$t_b = \frac{U_2}{b} = \frac{23.3}{2} = 11.65 \text{ [sec]}$$

$$t_c = T - t_b - t_a = 144 - 11.65 - 27 = 105.35 \text{ [sec]}$$

$$S_a = \frac{1}{2} t_a U_1 = 0.5 \times 27 \times 33.85 = 0.126 \text{ [mile]}$$

$$S_b = \frac{1}{2} t_b U_2 = 0.5 \times 11.65 \times 23.3 = 0.037 \text{ [mile]}$$

$$S_c = S_T - S_a - S_b$$

$$= 1 - 0.126 - 0.037 = 0.836 \text{ [mile]}$$



Calculation of speed time Curve

the attractive effort available for acceleration

$$f_a = f_T - f_r - f_g$$

$$102 w_e a = f_T - w r \pm 22.4 w G_i$$


$$a = \frac{1}{102 w_e} [f_T - w r \pm 22.4 w G_i]$$

r, f_T is a function in speed so if a is a simple function we can integrated it to give $(t-v)$ relation as

$$a = \frac{dv}{dt} \Rightarrow t = \int \frac{1}{a} dv$$

the above equation gives the time at certain speed under varying acceleration.

during coasting and braking a and dv are negative.

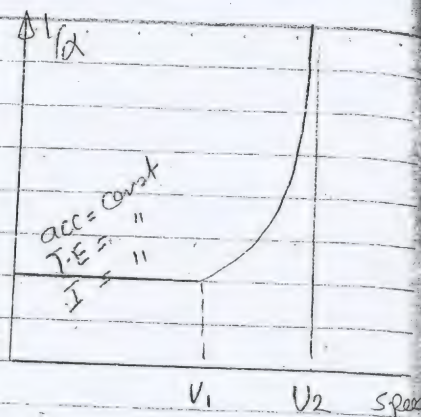
→ $\frac{dv}{dt} = -a$ 

$\frac{1}{a}$ is approximately const

up to speed v_1

$\frac{1}{a}$ increase to ∞ at speed

v_2



$v < \frac{1}{a}$

as resistance decreases

as resistance decreases

acceleration \propto (Speed-time)

(Ex) a train has total weight of 116 tons and has four motor each of 275 h.p

| Current (A) | 100 | 200 | 300 | 400 | 500 |
|-------------------------|-----|------|------|------|------|
| Speed (m.p.h) | 51 | 31.4 | 26.4 | 23.9 | 22.1 |
| T.E (lb.wt)/motor | 390 | 1600 | 2960 | 4330 | 5690 |
| train resistance lb/ton | 10 | 10 | 10 | 10 | 10 |

the ratio of effective weight to dead weight is 1.1 $I_{mean} = 425$ A per motor

braking retardation is $b = 2$ m.p.h.ps, $S = 0.86$

$T = 11.5$ sec, $G_i = 0.119$ train resistance during

Coasting is 10 lb.wt/ton, find I_{rms} per motor.



< Solution >

Draw (T.E - Current), (Speed-Current) curves.

as shown in fig (1).

the current not allowed to exceed 425 A (mean current)

so that the T.E max / motor is 4650 lb.wt

at speed 23.5 m.p.h. (from drawing).

$F_g = +22.4$ in G_i

$= 22.4 \times 0.119 \times 116 = 310$ (lb.wt)

$r = \text{const} \Rightarrow F_r = \text{const}$

find $F_T, F_r, F_g \propto 1/a$ against speed.

| speed | 23.5 | 26 | 28 | 30 | 35 | 40 | 45 |
|-------------------------|-------|-------|-------|------|------|-------|-------|
| F_T $4 \times F_m$ | 18400 | 12800 | 10000 | 7600 | 5000 | 3400 | 2200 |
| F_r | 1160 | | | | | | |
| F_g | 310 | | | | | | |
| F_a | 16930 | 12374 | 8530 | 6130 | 3530 | 1930 | 730 |
| a | 1.3 | 0.955 | 0.656 | 0.47 | 0.27 | 0.148 | 0.056 |
| $1/a$ | 0.769 | 1.1 | 1.52 | 2.12 | 3.68 | 6.7 | 17.8 |

to find F_t .

from drawing at speed we can find F_{motor} then we multiplying $F_m \times 4$

to find a :-

$$F_a = 102 \text{ we } a$$

$$a = \frac{F_a}{102 \text{ we}}$$

$$a = \frac{F_a}{13000} \quad (\text{m.p.h.p.s})$$

then find $\frac{1}{a}$

Draw $\frac{1}{a}$ with v .

the acceleration is constant at speed $v_1 = 23.5$

$$\frac{1}{a} \Big|_{23.5} = 0.767$$

to Draw speed time Curve:-

$$a = \frac{dv}{dt}, \quad dt = \frac{1}{a} dv, \quad t = \int \frac{1}{a} dv$$

with this as example, $\frac{1}{a}$ (V) we can find t in

$$\text{at } N = 23.5 \quad t = 23.5 \times 0.767 = 18 \text{ sec}$$

$$\text{at } N = 26 \quad t = 18 + \frac{1}{2} (1.1 + 0.767) \times 2.5 = 20.3 \text{ sec}$$

$$\text{at } N = 30 \quad t = 20.3 + \frac{1}{2} (1.1 + 2.12) \times 4 = 26.74 \text{ sec}$$

| | | | | | | |
|-------|---|------|------|-------|-------|-------|
| speed | 0 | 23.5 | 26 | 30 | 35 | 40 |
| time | 0 | 18 | 20.3 | 26.74 | 41.24 | 67.19 |

* to Draw braking curve (we draw straight line with slope = 2)

from $T = 115 \text{ sec}$ draw line with slope = 2

* to Draw coasting line.

supplying is off so the force is friction force and gravity force.

$$F_a = 0, \quad F_T = -f_r - f_g = 102 \text{ we } bc$$

$$bc = \frac{-f_r - f_g}{102 \text{ we}} = \frac{-1160 - 310}{102 \times 1.1 \times 116} = -0.113 \text{ m/s}$$

we cannot know the end of acceleration and starting of coasting so there are 2 ways:-

① given distance of run.

$$1 \text{ mm}^2 = 0.5 \text{ m.p.h} \times \frac{1 \text{ hour}}{3600}$$

$$1 \text{ mm}^2 = \frac{1}{7200} \text{ mile}$$

the total distance can be represented by

$$\frac{0.86}{1/7200} = 6192 \text{ mm}^2$$

6192 mm² is the total distance of run.

0.113 is the slope of the line.

25

$$S = 0.5(115 + 92) \times 10 = 520 \text{ mm}^2$$

at 20 m.p.h

$$S = 0.5(115 + 82) \times 20 = 985 \text{ mm}^2$$

at 30 m.p.h

$$S = 0.5(115 + 62) \times 30 = 1327.5 \text{ mm}^2$$

at 35 m.p.h

$$S = 0.5(115 + 45) \times 35 = 1450 \text{ mm}^2$$

at 37 m.p.h

$$S = 1530 \text{ mm}^2$$



From this point (37 m.p.h) Draw line with slope 0.113

② given $t_b = 15 \text{ sec}$

Jericho 100 sec, no 0.113 is the slope of the line.

Coasting line etc

* Plot (I-t) curve.

at $t > 45 \text{ sec} \Rightarrow I = 0$ acceleration is zero.

at $V = V_2 = 36 \text{ m.p.h}$ coasting line

find I from fig (1)

$$I = 175 \text{ (sec)}$$

at $V = V_1 = 23.5 \text{ m.p.h}$ I is the slope of the line.

$$I = 19 \text{ (sec)}$$

119

$$I_{rms} = \sqrt{\frac{1}{T} \int i^2 dt}$$

119

$$= \sqrt{\frac{1}{115} \left[(425^2 \times 19) + 0.5(45-19)(425^2 + 175^2) \right]}$$

3431675

10625

30625

2746250

$$I_{rms} = 230 \text{ A}$$

53772

Traction motors

divided to:

1. DC Motors

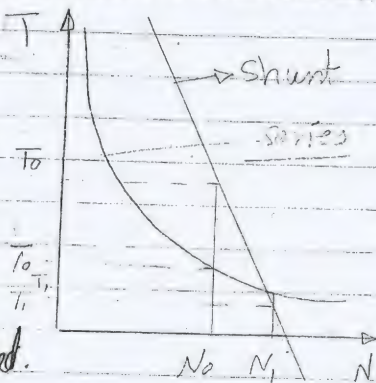
- Series
- Compound

2. AC Motors

- 1- ϕ I.m
- 3- ϕ I.m

* why series or compound motor most used in traction than shunt motor.

1. the series motor or compound have a torque-speed char. that show a rapid variation of speed with torque while the shunt motor has a small variation of speed with torque.



2. $N \propto \frac{1}{I}$, $N = \frac{V}{I} = \text{rotating speed}$.

at high speed shunt motor may be run as generator
-ve torque produced.



* Starting and speed control of DC motor.

Speed of dc motor can be varied by:

(i) Varying the field.

a. by tapping on the field.

b. by shunt resistance across it "field weakening"

(ii) Varying voltage applied.

a. series resistance method (notching)

b. Series parallel method

c. metadyne

d. word leanand system (not used in E.T)

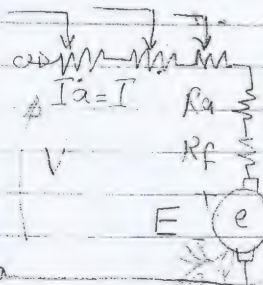
(a) Notching:

The Current in series motor given

$$E = V - IR_T, R_T = R_a + R_f + R_{ex}$$

$$I = \frac{E}{R + KN}, E = KNI$$

at $N=0 \Rightarrow I = \frac{V}{R_T}$ where R_T is small
so I_{st} is large.



So external resistance is inserted to limited I and we decrease R_{ex} gradually so until it go out of circuit the the current is

$$I = \frac{V}{K_1 N + R_a + R_f}$$

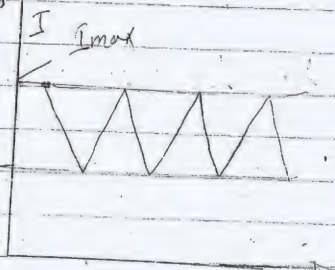
the current has a min & max value.

at $N=0$ $I = I_{max} = \frac{E}{R}$

$N = N_1$ $I = I_{min}$ I_{min}

$N = N_2$ $I = I_{max}$ (Reduced)

$N = N_3$ $I = I_{min}$



in this way we divided the current until we reach to full speed.

disadvantages: I_{max} I_{min} Limited للتيار

Copper loss

* decrease speed

limiting current

* advantages:

easy to use, Simple

reduce starting current, $Pf = 1.0$

الحل هو تقليل التيار في البداية ثم زيادته بالتدريج حتى يصل إلى السرعة المطلوبة

[2] Series-parallel Control (to decrease Copper loss)

in this method we deal with 2 motor

1- the 2 motor can be started in series with starting resistance until half speed and then the series resistance is zero so $E_1 + E_2 = V$ ($0 \rightarrow N/2$)

2- motor switched into parallel with limiting resistance again until full speed so

$$E_1 = E_2 = V \quad (N/2 \rightarrow N)$$

there are 2 method for transition from series to parallel.

[I] shunt transition:

1- the motor running at $N/2$ and series resistance is out

2- Some resistance is reinserted

3- one motor is short circuit

4- this motor has one end opened

5- then this end is connected across so that motors are in parallel.

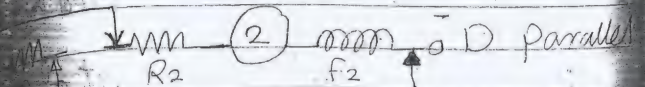
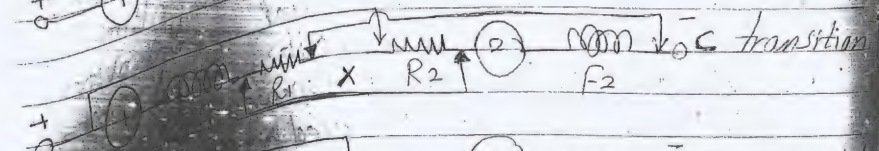
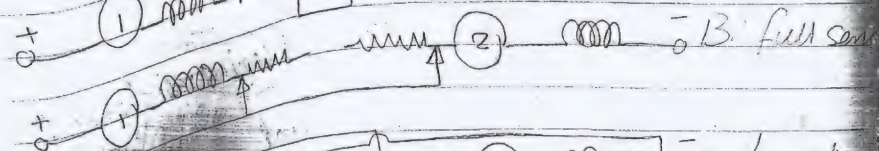
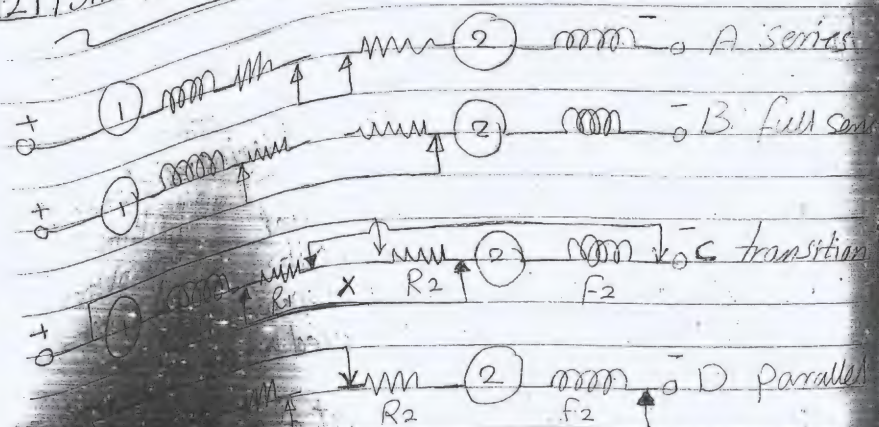
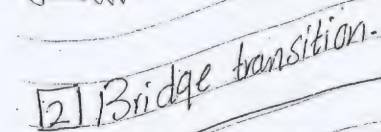
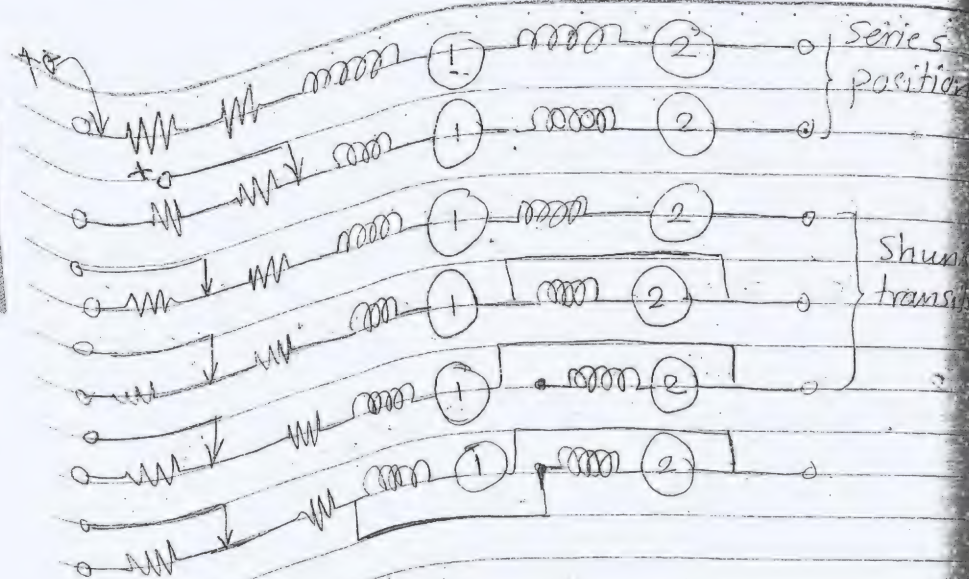
6- the series resistance is out of circuit.

* disadvantages:

1- there is a jerk in the system as one motor is shorted and another jerk when reinserted

due to K.E in motor.

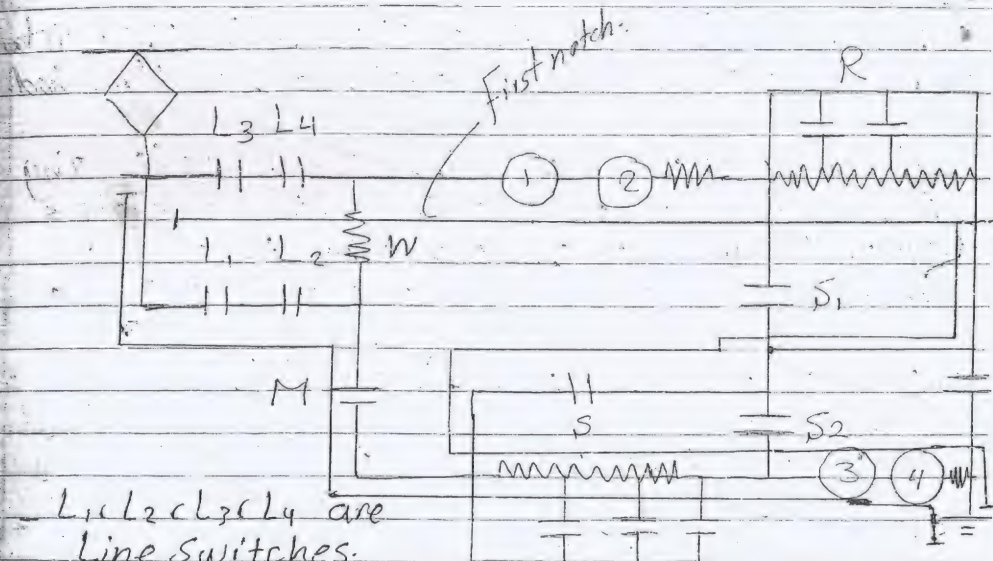




if the bridge is balance by
choosing a value of (R_1, R_2)

2. No current pass in branch (X)
So the transition is smooth
and there is no Jerk.

Simplified form of the Power diagramma 1500 volt
dc train equipment.



L_1, L_2, L_3, L_4 are Line Switches.

S1C S1C S1C Contactor R

W ~~is~~ resistance to protect the system at switch on in case there is a fault in motor 1.

* on the first notch.

L1, L2 & 5 closed then L3, L4 closed the motors are in series.

* S_1, S_2 closed & S open. motors still in series

* Contactor R then open & m.c.p are closed

Since S_1, S_2 are open so the motors are in parallel

with full limiting resistance.

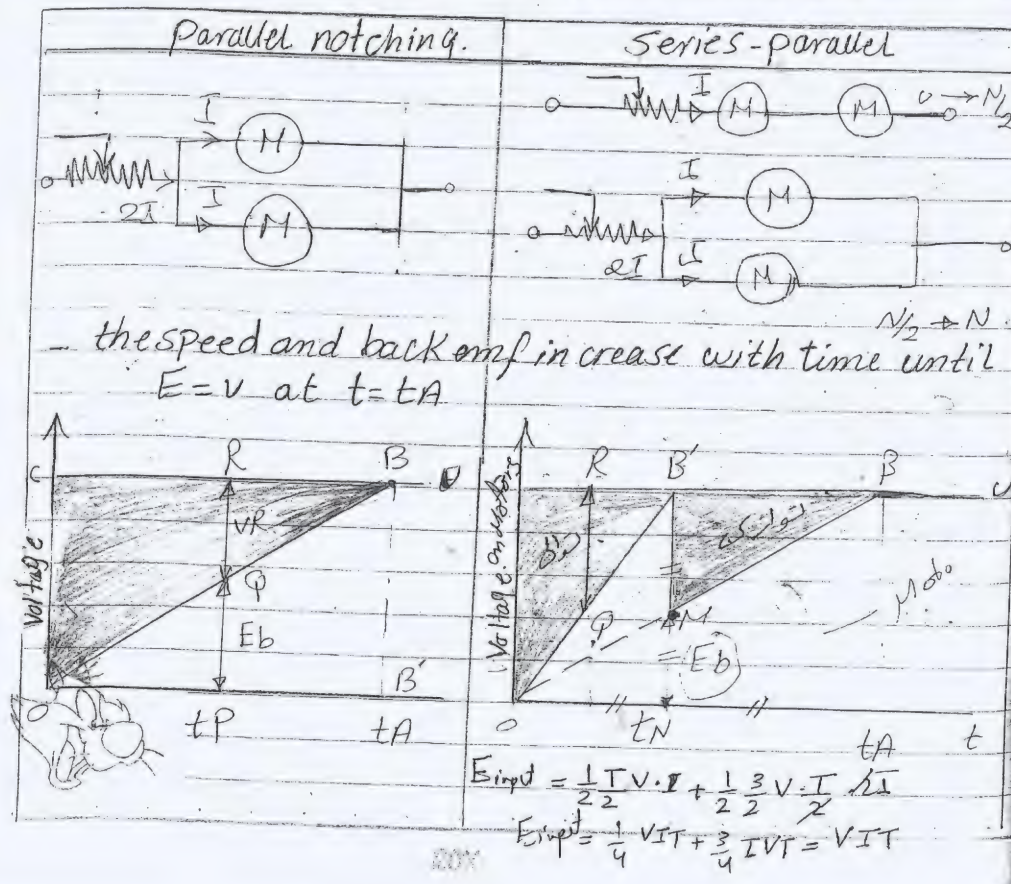
Energy saved By series parallel control.

there are 2 cases:

- 1) motors started in parallel with limiting resistance
- 2) motors started with series and parallel method.

in both cases we assume that the series limiting R are continuous varied so current in each motor equal to the max value whether in series or parallel so motors produce a constant torque

neglect armature and field resistance.



at $t = t_P$

$$E_b = \phi P$$

the drop on limiting resistance = ϕR

$$P_{loss} = 2 I \phi R$$

$$E_{loss} = \Delta \phi R \times 2 I$$

$$= 2 I (0.5 V t)$$

$$E_{loss} = I V t$$

input energy to motors =

$$= 2 I \times \Delta \phi R$$

$$= 2 I \times (0.5 V t)$$

$$E_{in} = I V t$$

$$\eta_{notch} = \frac{P_{out}}{P_{in}} \times 100 = \frac{P_{out}}{P_{out} + P_{loss}}$$

$$\eta_{notch} = \frac{I V t}{I V t + I V t} = 0.5$$

$$\eta_{notch} = 50\%$$

$$\therefore \eta_{s.p} > \eta_{notching}$$

* Energy wasted in series parallel is half that in notching

at $t = t_N$ the motor connected parallel

$$E_b = M N \text{ and drop on } R = M$$

in series mode the loss

$$E_{loss} = I \times \Delta \phi R$$

at $t = t_N$ motors switched in parallel so E_{loss} equal

$$E_{loss} = 2 I \Delta M B$$

$$E_{loss} = I \times \Delta \phi R + 2 I \Delta M B$$

$$= I (0.5 V t / 2) + 2 I (\frac{1}{2} V t / 2)$$

$$E_{loss} = 1/2 V t I$$

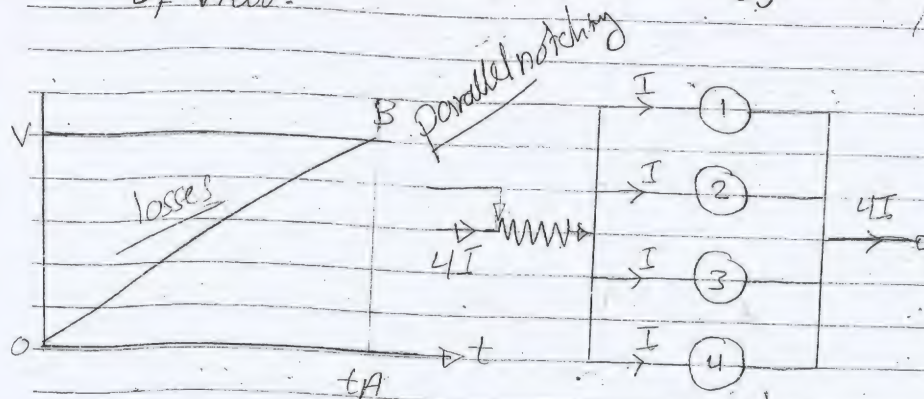
$$E_{loss}^{notch} > E_{loss}^{s.p}$$

$$\eta = \frac{I V t P_o}{s.p. I V t + 1/2 I V t}$$

$$\eta = 66 \frac{2}{3} \%$$

Ex there are 4 motor in train its desired to use a series parallel method to as follows.

- [1] Series [2] Series-parallel [3] Parallel Combination
there are 3 speed whose rating $1:2:4$
Compare between thus method and notching method of starting from efficiency and energy loss point of view.



$$E_{\text{losses}} = 4I \times \Delta OCB$$

$$= 4I \times (1/2 VT)$$

$$E_{\text{losses}} = 2IVT$$

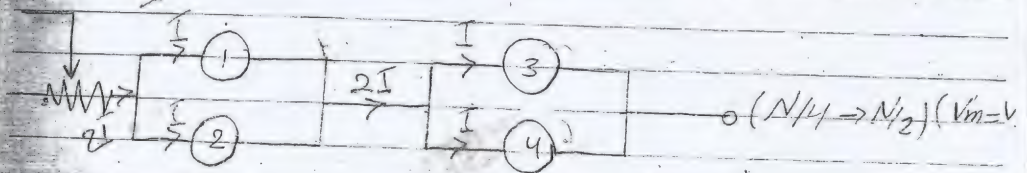
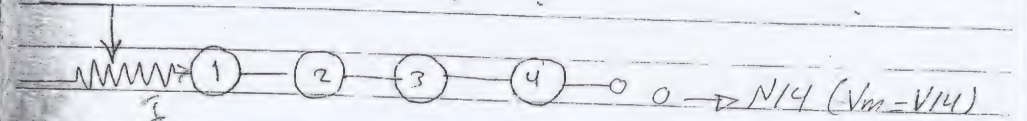
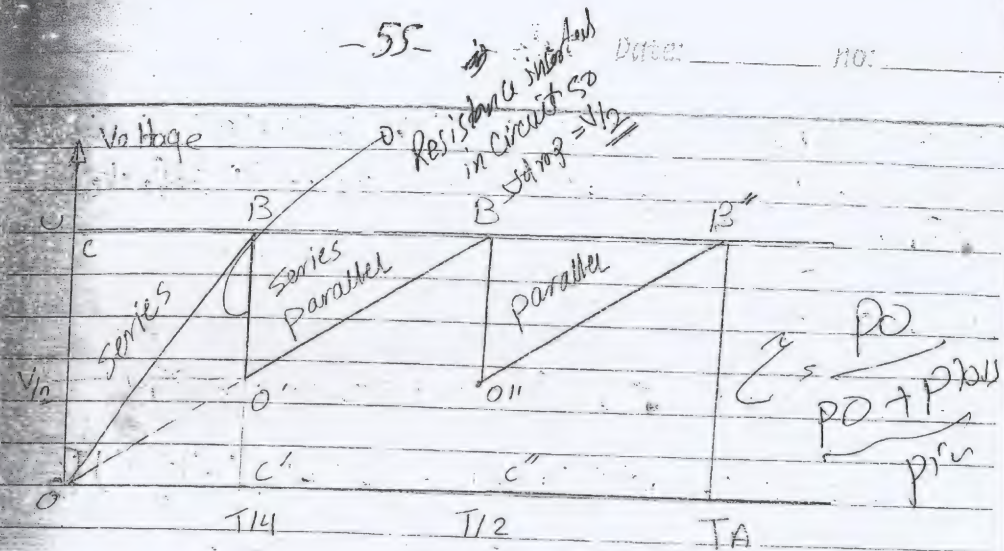
$$E_{\text{inp}} = 4I \times \Delta OCB$$

$$= 2IVT$$

$$\eta_{\text{notch}} = \frac{E_{\text{out}}}{E_{\text{out}} + E_{\text{loss}}} = \frac{2IVT}{2IVT + 2IVT} = 50\%$$



$$\eta_{\text{notch}} = 50\%$$



in series

each motor have $V/4$ $e_b = V/4$
and rotate to $N/4$

in series parallel

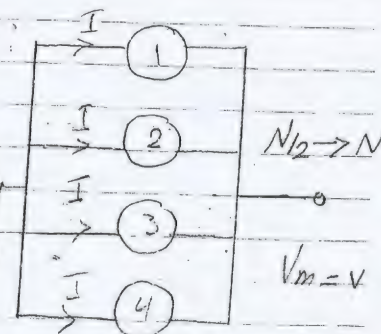
we insert resistance so

voltage on motor $V/2$ and $e_b = V/2$

the resistance is switched off gradually \therefore so motor rotate $N/2$

in parallel

insert resistance and switched off gradually so the voltage on motor is V and rotate " N "



$$E_{loss} = I \Delta OCB + 2I \Delta O'BB' + 4I \Delta O''BB''$$

$$= I(0.5V T/4) + 2I(0.5V/2 T/4) + 4I(V/2 T/2 * 1/2)$$

$$(E_{loss} = 0.75 IVT)$$

input energy:

$$= I \Delta OBC' + 2I \Delta O'BC''C' + 4I \Delta \text{area } C''O''B''M$$

$$= I(0.5V T/4) + 2I(V+0.5V T/4) + 4I(V+0.5V T/2)$$

$$= \frac{IVT}{8} + \frac{3IVT}{8} + \frac{3IVT}{2}$$

$$= 2IVT$$

$E_{in} = E_{out} \text{ of motors} = \text{Energy used}$

$$\eta_{slp} = \frac{E_{out}}{E_{in} + E_{loss}} = \frac{2IVT}{2IVT + 0.75IVT} = 0.73$$

$$\eta_{slp} = 73\%$$

$$\eta_{slp} > \eta_{noth} \quad \#$$

$$\frac{E_{loss}}{E_{used}} = \frac{0.75IVT}{2IVT} = 0.375$$



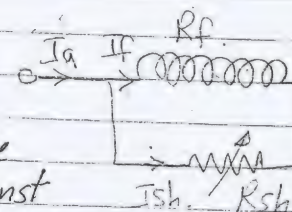
Field weakening or tapped field control.

using tapping

by tapping field winding to change I_f and so on change flux.

using shunt resistance

the armature current is const but as R_{sh} change I_{fsh} change and so I_f change to have $I_a = \text{const}$

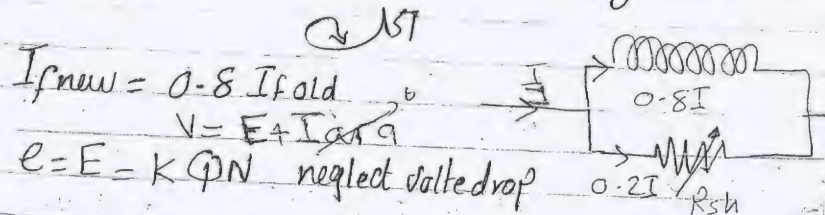


Ex

The following figures relate to a series-wound motors of an electric locomotive.

| Current Per motor (A) | 200 | 300 | 400 | 500 |
|------------------------------|------|------|------|------|
| Train speed (m.p.h) | 41.5 | 33.5 | 28.5 | 28.0 |
| Tractive effort / motor (lb) | 1300 | 2460 | 3660 | 4870 |

Calculate the value of speed and T-E for the same range armature current when a series field current reduced by 20% by a field diverting resistance.



$$I_{fnew} = 0.8 I_{fold}$$

$$V = E + I_a R_a$$

$$E = E - K \phi N \quad \text{neglect voltage drop}$$

if supply voltage is const $N \propto \frac{1}{\phi}$ $\phi \propto I_f$

the relation between speed and current it is not Linear.

$$I_a = \text{const} \quad I_a = I_f + I_{fs} = \text{const}$$

$$\text{at } I_a = 500 \text{ A} \Rightarrow I_{f \text{ new}} = 0.8 \times 500 = 400 \text{ A} \Rightarrow N = 28.5$$

$$\text{at } I_a = 400 \text{ A} \Rightarrow I_{f \text{ new}} = 0.8 \times 400 = 320 \text{ A} \Rightarrow N = 32$$

$$\text{at } I_a = 300 \text{ A} \Rightarrow I_{f \text{ new}} = 0.8 \times 300 = 240 \text{ A} \Rightarrow N = 38$$

$$\text{at } I_a = 200 \text{ A} \Rightarrow I_{f \text{ new}} = 0.8 \times 200 = 160 \text{ A} \Rightarrow N = 45$$

$$N \propto \frac{1}{I_f}$$

من سرعة الدوران (N) إلى التيار (I_f)

$$* T.E \propto I \phi \quad \phi \propto \frac{1}{N} \Rightarrow T.E \propto \frac{I}{N} \text{ at const } E$$

- relation between T.E and I_a from curve is nearly Linear So

$$T.E_{\text{new}} = T.E_{\text{old}} \times \frac{N_{\text{old}}}{N_{\text{new}}}$$

$$\text{at } I_a = 500 \text{ A}$$

$$T.E = 4870 \times \frac{28}{28.5} = 4784.56 \text{ (ib)}$$

$$\text{at } I_a = 400 \text{ A}$$

$$T.E = 3660 \times \frac{28.5}{32} = 3260 \text{ (ib)}$$

$$\text{at } I_a = 300 \text{ A}$$

$$T.E = 2460 \times \frac{33.5}{38} = 2168 \text{ (ib)}$$

$$\text{at } I_a = 200 \text{ A}$$

$$T.E = 1300 \times \frac{41.5}{45} = 1198.9 \text{ (ib)}$$

Draw the new Curves.

| Current per motor (A) | 200 | 300 | 400 | 500 |
|---------------------------|--------|------|------|---------|
| train Speed (m.p.h) | 45 | 38 | 32 | 28.5 |
| tractive effort per motor | 1198.9 | 2168 | 3260 | 4784.56 |

* find an expression for specific energy consumption (S.E.C)

$$S.E.C = \frac{\text{energy consumption (W.hr)}}{W.S}$$

W \Rightarrow dead weight, S \Rightarrow length of train

$$S.E.C \text{ for acceleration} = \frac{1/2 P a t_a}{W.S}$$

$$S.E.C A = \frac{1/2 (0.002) \times 102 \text{ W} \times V \sqrt{1/g}}{W.S} \quad \text{Kw.sec / ton mile}$$

$$= 0.102 \frac{\text{W} \text{eV}^2}{W.S} \quad \text{Kw.sec / ton mile}$$

$$S.E.C A = 0.028 \frac{\text{W} \text{eV}^2}{W.S} \quad \text{W.h / ton mile}$$

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Energy consumption for acceleration = $\frac{1}{2} P a t a$

$$= \frac{1}{2} P a t a = 0.028 \text{ we } V^2 \quad (\text{w.h})$$

[2] S.E.C for overcome train resistance.

$$S.E.C.R = \frac{2 F r S'}{W S} = \frac{2 W r S'}{W S}$$

$$S.E.C.R = 2 r \frac{S'}{S} \quad (\text{w.h / ton-mile})$$

where

$$S' = \frac{1}{2} t a V_m + t c V_m \rightarrow \text{Free running}$$

$$S' = \frac{1}{2} t a V_m \rightarrow \text{without free running}$$

energy consumption for resistance = $2 F r S'$ (w.h)

[3] S.E.C.G (energy consumption to overcome gradient gravity)

$$S.E.C.G = \frac{2 F g S'}{W S}$$

$$= \pm 2 \times 22.4 W G i S'$$

$$S.E.C.G = \pm 44.8 \frac{G i S'}{S}$$

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$$G_i = 100 \sin \theta$$

energy consumption for gradient gravity

$$= 2 F g S' \quad (\text{w.h})$$

Sheet(11)

(6) 2 stations 1 mile apart, $S = 10 \text{ mile}$, $V_{av} = 25 \text{ m.p.h}$ & $= 27.5 \text{ m.p.h}$

total weight = 210 tons

acceleration = 1.2575 m.p.h.p.s

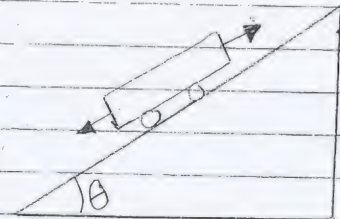
braking retardation = 2 m.p.h.p.s

net T.E = 30000 Ib up

" " = 47000 Ib down

$r = 12 \text{ Ib}$

$w_e = 1.1 w$



assume both direction made to trapezoidal speed time curve and determine without free Run.

<< Solution >>

Specific energy output = specific energy consumption

S.E.C = energy need to accelerate train

+ " " " overcome " resistance

+ " " " " gravity

acceleration

retardation

$$f_t = f_a + f_r + f_g \quad \text{up} \rightarrow a_{up} \quad f_t = f_a - f_r - f_g \quad \text{up} \rightarrow b_{up}$$

$$f_t = f_a + f_r - f_g \quad \text{down} \rightarrow a_{down} \quad f_t = f_a - f_r + f_g \quad \text{down} \rightarrow b_{down}$$

① S.E need to accelerate the train

$$S.E.C.A = \frac{1/2 P a t a}{w.s}$$

$$= \frac{1}{2} \frac{0.002 F a v \sqrt{1 a}}{w.s}$$

$$S.E.C.A = 0.028 \frac{w e v^2}{w.s} \quad w.h / \text{ton mile}$$

② S.E need to overcome the train resistance

$$S.E.C.R = \frac{2 f r s'}{w.s} = \frac{2 r s'}{s} \quad \# \quad w.h / \text{ton mile}$$

$$s' = 0.5 t a v_m + t c v_m \checkmark$$

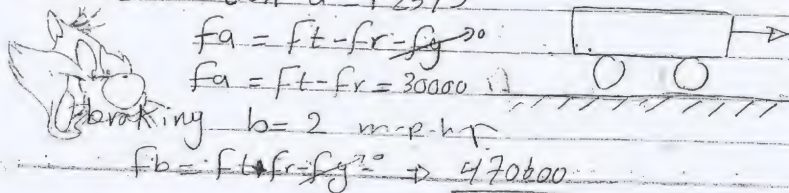
$$s' = 0.5 t a v_m$$

③ S.E need to overcome gradient gravity

$$S.E.C.G = \frac{2 f g s'}{w.s} = \pm 2 \times 22.4 W G i s'$$

$$S.E.C.G = \pm 44.8 \frac{G i s'}{s} \quad \#$$

acceleration $a = 1.2575$



1) for acceleration the train

$$f_a = f_t - f_g - f_r$$

$$102 w e d u p = f_t - f_g - f_r$$

$$d u p = \frac{f_t - f_g - f_r}{102 w e} = \frac{30000 - (22.4 \times 210 \times \frac{100}{80})}{102 \times 231}$$

$$d u p = 1.02 \text{ [m.p.h.p.s]}$$

$$\alpha_{down} = \frac{f_t + f_r + f_g}{102 w e} = \frac{30000 + (22.4 \times 210 \times \frac{100}{80})}{102 \times 231}$$

$$\alpha_{down} = 1.523 \text{ m.p.h.p.s}$$

$$f_b = f_t - f_r - f_g$$

$$b = \frac{f_t + f_r - f_g}{102 w e}$$

$$b u p = \frac{f_t + f_r + f_g}{102 w e} = \frac{47000 + (22.4 \times 210 \times \frac{100}{80})}{102 \times 231}$$

$$b u p = 2.244 \text{ m.p.h.s}$$

$$b_{down} = \frac{f_t + f_r - f_g}{102 w e} = \frac{47000 - (22.4 \times 210 \times \frac{100}{80})}{102 \times 231}$$

$$b_{down} = 1.745 \text{ m.p.h.p.s}$$

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Date:

no:

$$V_{up} = \frac{1}{2K} \left[T - \sqrt{T^2 - 14400SK} \right]$$

$$K_{up} = \frac{1}{2a_{up}} + \frac{1}{2b_{up}} = \frac{1}{2 \times 1.02} + \frac{1}{2 \times 2.244}$$

$$K_{up} = 0.713$$

$$U_{av} = \frac{S}{T_{up}}, T_{up} = \frac{S}{U_{av}} = \frac{1}{25} = 144 \text{ Sec}$$

$$U_{up} = 29.23 \text{ m.p.h}$$

$$* T_{down} = \frac{1}{27.5} = 0.036 \text{ hr} = 131 \text{ sec}$$

$$K_{down} = \frac{1}{2a_{d}} + \frac{1}{2b_{down}} = \frac{1}{2 \times 1.523} + \frac{1}{2 \times 1.745}$$

$$K_{down} = 0.615$$

$$V_{down} = \frac{1}{2 \times 0.615} \left[131 - \sqrt{131^2 - 14400 \times 0.615 \times 1} \right]$$

$$U_{down} = 32.4 \text{ m.p.h}$$

$$t_{a up} = \frac{U_{up}}{a_{up}} = 28.65$$

$$t_{b up} = 13.025$$

$$t_{cup} = T - t_{a up} - t_{b up} = 102.3$$

$$t_{a down} = 21.27 \text{ sec}$$

$$t_{b down} = 18.567 \text{ sec}$$

$$t_{c down} = 91.2 \text{ sec}$$

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Date:

no:

* for up gradient direction

$$S.E.C.A = 0.028 \frac{W_e V^2}{W.S} = 0.028 \times \frac{231 \times 29.23^2}{210}$$

$$S.E.C.A = 26.3 \text{ w.h/ton mile}$$

$$S.E.C.R = \frac{2rS'}{S} = 2r \times \left(\frac{1}{2} \tan \alpha \right)$$

$$S' = \frac{1}{2} \frac{29.23^2}{3600 \times 1.02} = 0.11 \text{ m/s}$$

$$= \frac{2 \times 12 \times 28.65 \times 29.23}{2 \times 3600} = 2.8 \text{ w.h/ton mile}$$

$$S.E.C.G = +44.8 \frac{G' S'}{S} = 44.8 \times \frac{100}{80} \times 0.5 \times \frac{28.65 \times 29.2}{3600}$$

$$= 6.5 \text{ w.h/ton mile}$$

$$S.E.C = 6.5 + 2.8 + 26.3 = 35.6 \text{ w.h/ton mile}$$

* for down gradient direction

$$S.E.C.A = 0.028 \frac{W_e V^2}{W.S} = 32.3 \text{ w.h/ton mile}$$

$$\rightarrow 0.0957 \text{ m/s}$$

$$S.E.C.R = \frac{2rS'}{S} = 2.3 \text{ w.h/ton mile}$$

$$S.E.C.G = -44.8 \frac{G' S'}{S} = -5.36 \text{ w.h/ton mile}$$

$$S.E.C = 29.2 \text{ w.h/ton mile}$$

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$$bc = \frac{V_1 - V_2}{ts}$$

visif

$$U_2 = U_1 - bctc$$

$$U_2 = 38 - 0.1tc \rightarrow \bullet$$

$$tb = \frac{V_2}{b} \Rightarrow V_2 = btb \rightarrow \bullet$$

$$\therefore tb = 19 - 0.05tc$$

From 1.2

$$ta = T - ta - tb$$

$$ta = 150.2 - 19 + 0.05tc - tc$$

$$ta = 131.2 - 0.95tc \rightarrow \bullet$$

$$S = 1.2 = \frac{1}{7200} \left[\underbrace{4985}_{S_a} - 36tc + \underbrace{(76 - 0.1tc)}_{S_b} tc + (38 - 0.1tc)(19 - 0.05tc) \right]$$

$$8640 = 4985.6 - 36tc + 76tc - 0.1tc^2 + 722 + 0.005tc^2 - 38tc$$

$$8640 = 0.095tc^2 + 36.2tc + 5707.6$$

$$0.095tc^2 - 36.2tc + 2932.4 = 0$$

$$tc^2 - 381.05tc + 30867.368 = 0$$

$$tc_1 = 264.229 \text{ sec}, tc = 116.82 \text{ sec} \checkmark$$

$$ta = 20.24 \text{ sec}$$

$$tb = 13.16 \text{ sec}$$

$$U_2 = 26.32 \text{ sec}$$



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$$S.F. \text{ out for the run} = 0.0283 \times \frac{r_1^2}{S} \frac{we}{w} + 2(r + 22.4G_1) \frac{S'}{S}$$

$$= 0.0283 \times \frac{38^2}{1.2} \frac{220}{200} + 2(10 + 0) \times \frac{0.5 \times 38 \times 20.24}{(3600 \times 1.2)}$$

$$G_1' = 0$$

$$S.F.C = 37.96 \text{ (wh / ton mile)}$$

(b) energy dissipated during coasting

$$E = \frac{1}{2} we V_1^2 - \frac{1}{2} we V_2^2 -$$

$$= \frac{1}{2} 220 \times (38)^2 - \frac{1}{2} \times 220 \times (26.32)^2 = 823783 \text{ (wh)}$$

(c) energy dissipated during braking

$$E = \frac{1}{2} we V_2^2 = 76201.66 \text{ wh}$$

(d) mean train resistance during coasting

$$bc = \frac{-fr - fg^{\circ}}{102we} = \frac{-fr}{102we}$$

$$-0.1 = \frac{-wr}{102we}$$

$$wr = 2244 \text{ lb-wt}$$

$$r = 11.22 \text{ lb/ton}$$

13] $w = 200 \text{ ton}$, Gross T.E = 25000 Ib, $S = 0.8 \text{ mile}$
 $T = 120 \text{ sec}$, up gradient, $r = 10$, $w_e = 1.1 w$
 $b = 2.2$

- required

Determine the maximum speed attained
 energy supplied to the driving wheels.

$f_a = f_t - f_r - f_g$

$102 w_e a = f_t - f_r - f_g$

$a = \frac{f_t - w_r - 22.4 w G'}{102 w_e}$

$f_t \Rightarrow$ gross tractive effort = 25000 Ib

$f_r = w_r = 200 \times 10 = 2000 \text{ Ib} \cdot \text{wt}$

$f_g = 22.4 w G' = 22.4 \times 200 \times \frac{100}{100} = 4480 \text{ Ib} \cdot \text{wt}$

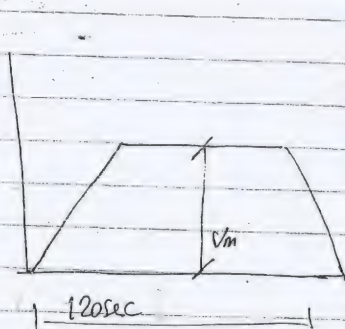
$K = \frac{1}{2a} + \frac{1}{2b} = \frac{1}{2 \times 0.825} + \frac{1}{2 \times 2.2}$

$K = 0.833 \checkmark$

$V = \frac{1}{2K} \left[T - \sqrt{T^2 - 14400 \times S \times K} \right]$

$V = \frac{1}{2 \times 0.833} \left[120 - \sqrt{120^2 - 14400 \times 0.8 \times 0.833} \right]$

$V_{\max} = 30.426 \text{ mph}$



$SEC = 0.028 \frac{V^2 w_e}{S w} + 2 (r + 22.4 G') \frac{S'}{S}$

$SEC = 0.0283 \times \frac{(30.426)^2}{0.8} \times \frac{220}{200} + 2 (10 + 22.4 \times 1) \frac{S'}{S}$

$S' = \frac{1}{2} t a V_m = \frac{1}{2} \frac{V_m^2}{a} = \frac{561.055}{3600} \text{ mile} = 0.155$

$S.E.C = \frac{148.8}{148.8} (W \cdot h / \text{mile ton})$

energy supplied to driving wheel = $S.E.C \times W \times S$
 $= 694.94 \text{ Wh} \quad 7808.0 \text{ Wh}$

10 | $t = 70 \text{ sec}$

| | | | | | | |
|-------------|------|------|------|------|------|------|
| Time (sec) | 0 | 10 | 20 | 35 | 50 | 70 |
| Speed m.p.h | 0 | 10 | 20 | 30 | 40 | 50 |
| ϵ | 0.25 | 0.18 | 0.14 | 0.12 | 0.10 | 0.09 |

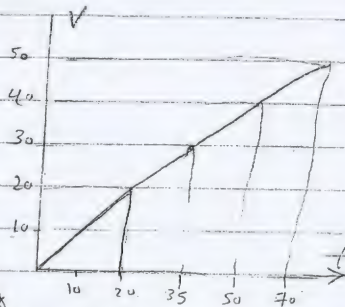
find U_{av} , ϵ_{av} ??

find maximum acceleration

SI

Draw (U-t), (ϵ -t)

$$U_{av} = \frac{S}{T} \text{ (area under curve)}$$



$$= \frac{1}{70} \left[0.5(20 \times 20) + 0.5(20+30) \times 15 + \frac{1}{2}(40+50) \times 20 + 0.5(30+40) \times 15 \right]$$

$$U_{av} = 28.67 \text{ [m.p.h]}$$

$$\epsilon_{av} = \frac{\text{area}}{T}$$

$$= \frac{1}{70} \left[0.5(0.25+0.18) \times 10 + 0.5(0.18+0.14) \times 10 + 0.5(0.14+0.12) \times 15 + 0.5 \times 35(0.12+0.09) \right]$$

$$\epsilon_{av} = 0.1339$$

$$f_t = \epsilon_{ad} \times W$$

$$m \times a = \epsilon_{ad} \times m \times 32.2 \text{ ft/sec-sec}$$

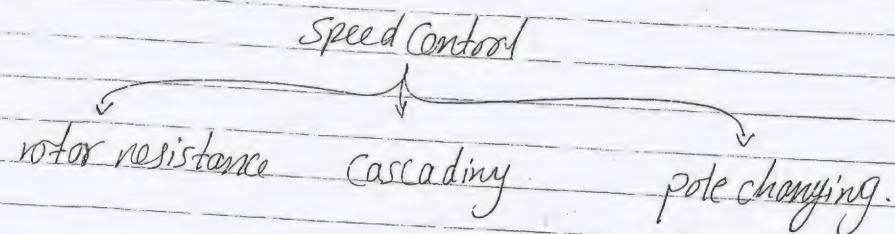
$$a \leq 0.25 \times \frac{32.2 \times 3600}{59.50} \text{ m.p.h.s}$$



* Starting of AC Motors and speed control.

[1] 3 phase Induction motor.

- for slip ring rotor starting is done by liquid or metallic rheostats in rotor circuit.



① rotor resistance

$$S = \frac{N_s - N}{N_s} = 1 - \frac{N}{N_s}$$

$$\frac{N}{N_s} = 1 - S, \quad N = (1 - S)N_s \quad \text{or} \quad N = \frac{60f}{p} \text{ rpm}$$

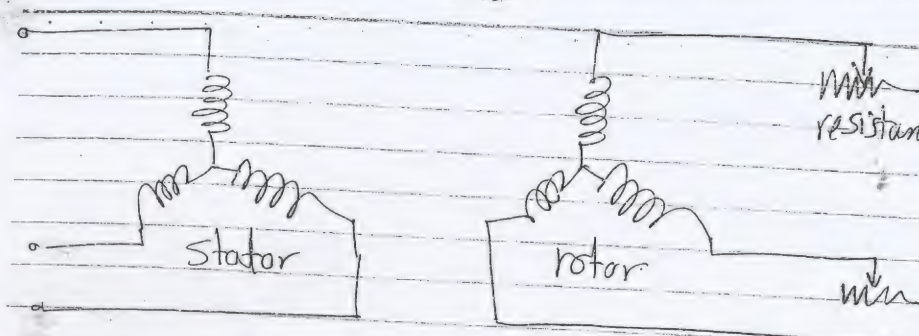
$$N = \frac{60f}{p} \text{ rps}$$

$$N = (1 - S) \frac{60f}{p} \quad \text{change } f, p, S \text{ to change speed}$$

$$\text{rotor copper loss} = s P_g = s \frac{K F T}{p} \rightarrow \text{torque}$$

if rotor copper loss changed $S \rightarrow$ change so N change

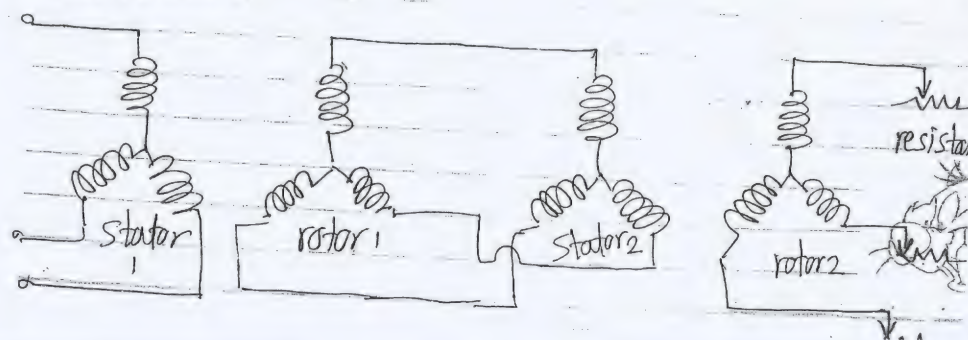
So we use resistance into rotor circuit to speed control.



this method has high (wasteful) losses (large copper losses) \Rightarrow more heat so the power can be used to operate another I.M cascading

[2] cascading I.M

- instead of power wasted into resistance this power can be used to operate another I.M by cascading connection



disadvantages

1- low power factor of Combination

2- require 2 3phase I.m

* the power is taken by aslip ring of the first motor to drive the second motor (SPg).

the rheostat in the second motor enable speed regulation up to the cascade synchronous speed

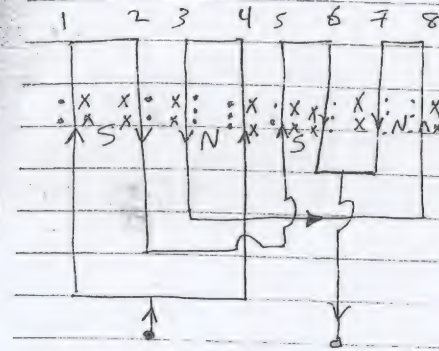
$$P_1 = 5P_2 \quad \text{pairs of poles}$$

$$N = \frac{120f}{P_1 + P_2} \quad \text{rpm}$$

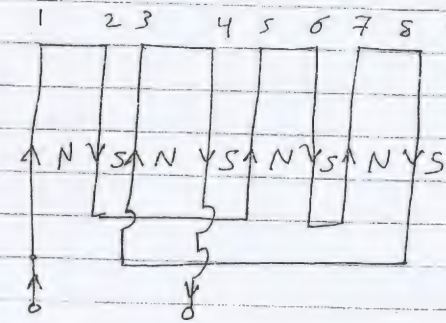
two motors are coupled Mechanical

If $P_1 = P_2$, $N = \frac{120f}{2P_1}$ so N half one motor speed, and 2 motor provide equal mechanical power.

3. Pole changing:



* 4 pole winding



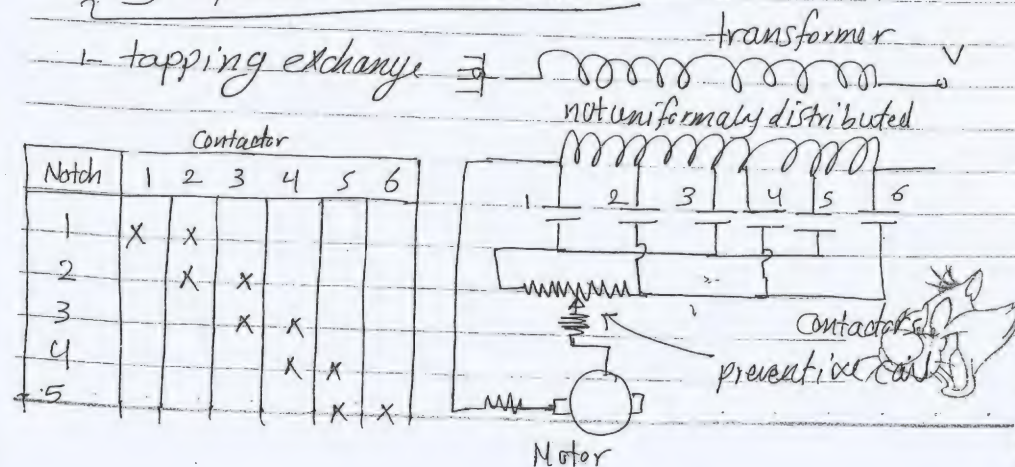
* 8 pole winding

$N = (1-s) \frac{120f}{P}$ as No of pole changed the speed changed

winding is connected to give 4 and 8 poles by altering supply connection

* Single phase Induction motor:

1- tapping exchange



there are five notch at each position two Contactors are closed.

the Volt Can be reducing at start without aresistance so large saving in energy.

the motor take its power from transformer secondary through tap exchange by acontactors.

* Preventive coil:-

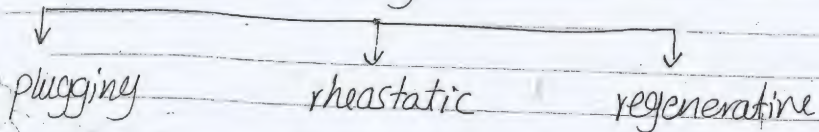
to ensure proper operation to prevent short circuit at transformer secondary.

at each notch there are two contactor closed.

* advantages:-

each notch is a running position so wide speed change low losses because high efficiency transformer.

* Electric braking



in certain train there are mechanical or electric wheel brakes.

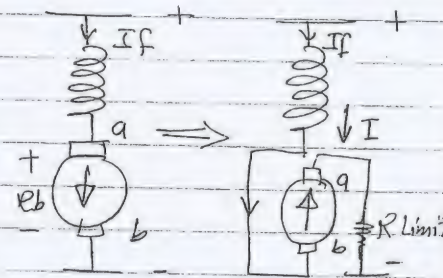
[1] Plugging:-

in plugging the torque is reversed by reverse of armature current or field current.

but not (both). its better

to current (I_a) this for dc

Motor.



* it has high copper loss in series resistance. for three phase I.M plugging can happen by reversing direction of rotation of magnetic field by reversing one phase.

$$T = \frac{E + e_b}{R_a + R_{Limit}}$$

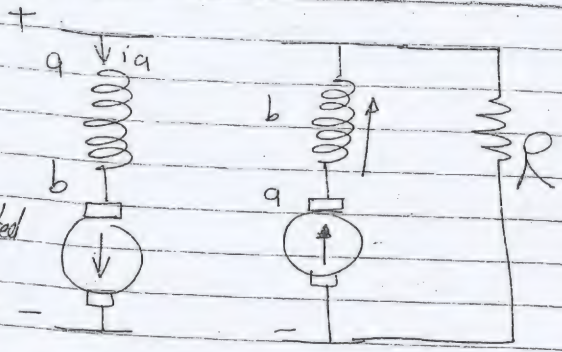
$$R_a + R_{Limit}$$

Construction is simple (advantages).

[2] * rheostatic braking:-

the motor is disconnected from the supply and connected to aresistance the kinetic energy that motor gain through running is dissipated through resistance and motor act as generator.

- in electric traction
there are 2 ~~or~~ 4
motors when we connected
in series and rheostatic -



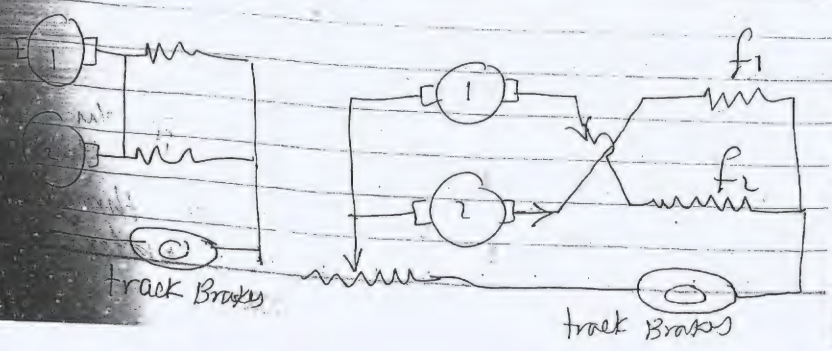
brake is applied the total voltage will be large so we
should connected it parallel to make brake.
so these motor should shared load equally.

* problem during this:-

one machine do build up fastly than other machine
so a short circuit may happen.

- there are 2 method to avoid short circuit condition

- 1- using an equalizing bar
- 2- across connection of the field



The armature current of the more power full excited
machine (fast build up) increase the field of the less
power full excited machine so the 2 M/cs have equal
excitation.

* advantages:-

1- low loss in energy because there isn't energy down
from supply at braking.

rheostatic braking is better than plugging because
plugging has much loss (energy from supply = VI and
the internal energy has to be dissipated into series
resistance so it has much wast in energy).

2- Simple in construction.



* Regenerative Braking:

* advantages and disadvantages of regenerative Braking on level route ??

* disadvantages:

- 1- So far as dc equipments are concined are briefly.
- 2- the motors are larger, heavier and more cost than ordinary equipments.
- 3- increase the maintenance charges on the electrical equipment
- 4- Control and operation become complicated.
- 5- increase weight of the train and no of motor
- 6- additional equipment to control the regenerative action of the motors.

* advantage:

- 1- reduce energy consumption
- 2- " wear or brake shoes and wheel tyres so lower maintenance cost of these parts.
- 3- small amount of brake dust produce when the mechanical brakes is applied.
- 4- reduction of energy consumption reach to 10% on level route but in undulating routes the saving may reach to 20%.

* Electric Regenerative on main line and mountain Railways

is essential due to:-

- 1- the large amount of energy available during the descent of the gradients.
- 2- the large use of electric locomotives
- 3- the operating conditions permitting the use of motor having a constant speed characteristics.
- 4- the running cost have to be found to be only about 75% of those when the lines were operated with steam locomotive through down gradients.
- 5- the recuperated energy being in order of from 60-80 of the energy consumption for the up journey with the same train.

* French method of Regenerative braking:

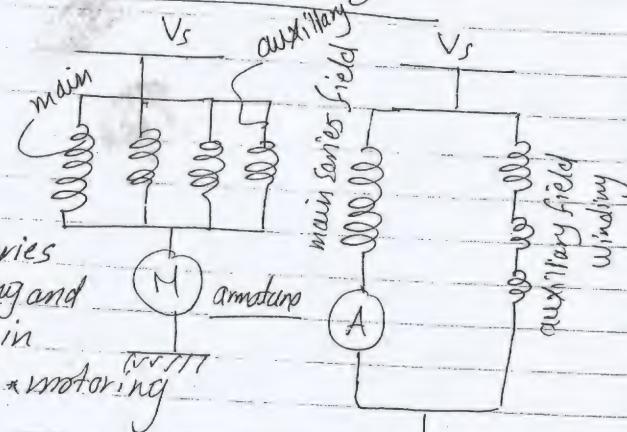
for one motor

* during motoring:

- the machine act as series motor the field winding and auxiliary winding are in parallel with it

* during generation:

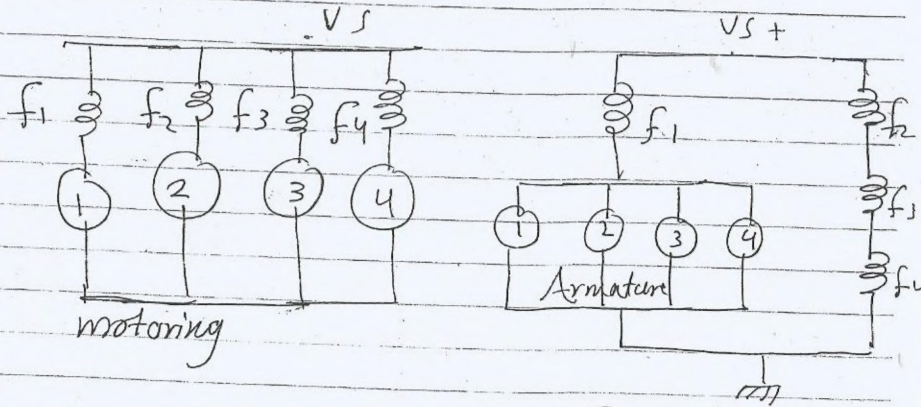
- the auxiliary winding are switched in series and the machine act as a shunt generation.



* For several motor:-

- during motoring: the field windings are in series with their own armature
- during generation: the motor circuit are in parallel (all armature in parallel)
- in series with one field winding and other field winding works as auxiliary winding (in series) parallel to one field winding and motor circuit.

* assume four motors.



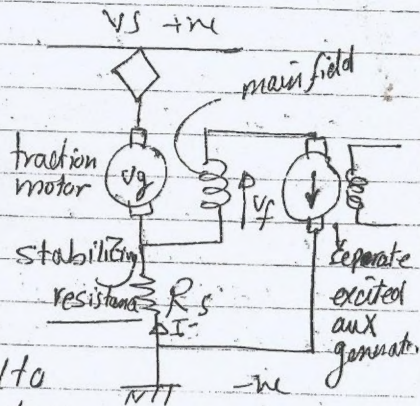
- the auxiliary winding connecting across the supply to help the main field winding to do build up fastly to return power to supply through braking.

* advantage:-

- there is not need any for auxiliary winding because some field winding ~~are~~ do its operation.

[2] metropolitan-vickers regenerative system:-

- this system use an auxiliary generator it can be either one of train motor or special HIC
- the magnitude of the regenerative current is controlled by varying the field strength of auxiliary generator



- the stabilizing resistance is used to
 - 1- prevent current surges when the motor crosses from one section of supply to another.
 - 2- to compensate for variable line volt.

$$v_g = v_s + I R_s$$

$$I R = v_g - v_s$$

$$I = I + I_{au}$$

$$V_{au} = v_f + I R_s$$

V_{au} is const as a separately Generator.

if V_s increase $\Rightarrow I \downarrow \Rightarrow I' \downarrow \Rightarrow I' R_s \downarrow \Rightarrow v_f \uparrow \Rightarrow v_g \downarrow$

* steps:-

- regenerative braking used down to about 10 m.p.h.
- the rheostatic braking down to 4 mph and finally mechanical braking until stand still 0 m.p.h.

3 Metadyne:

it is a method of varying volt by achieves smooth control of speed and starting of dc/MIC without dissipating energy in a resistance.

it's a rotating transformer for dc power with variable turn ratio. so it can draw power from dc source and deliver it at a constant current and variable voltage to an accelerating motor.

Fig(a):

ordinary machine with two poles and two brushes

Fig(b):

metadyne with four pole and four brushes

- $I_1 \Rightarrow$ produce primary flux
this primary flux produce emf between (B,D) brushes.
- I_2 flow through load.

Fig(c): I_2 produce a secondary flux this secondary flux produce emf between (A,C) brushes which neutralize the applied voltage (E_1)

from fig(b) $E_2 = K I_1$ neglect loss

$$E_1 = K I_2$$

$K \rightarrow$ constant depend on construction of MIC and speed

$$E_1 I_1 = E_2 I_2$$

input and output power are equal (like transformer)

if E_1 is const, $I_2 = \text{const}$ and load resistance change

$I_2 = \text{const}$, I_1 increase and E_2 increase.

عندما يظل الجهد E_1 ثابتاً، I_2 ثابتاً وتغير مقاومة الحمل

في هذه الحالة I_2 قيمة ثابتة ولكن I_1 تزداد و E_2 تزداد

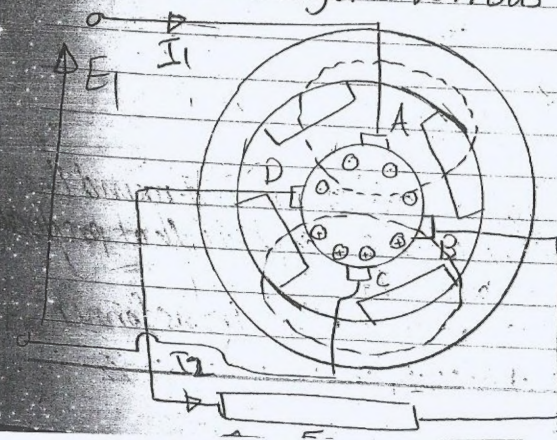
↓ Variator or regular winding.

advantage:

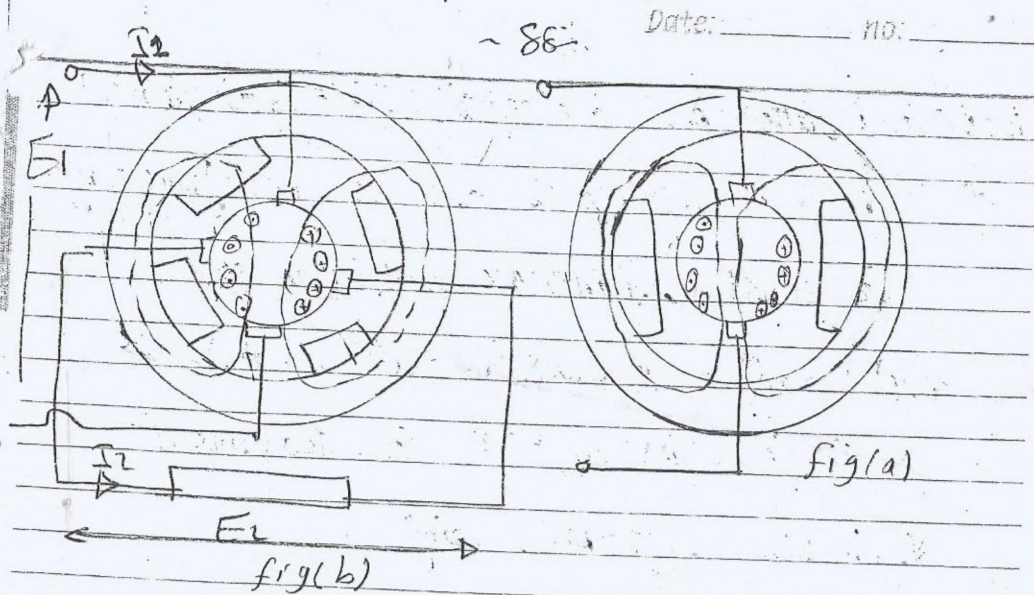
- no switch require so there is no surge appear
- low loss and high efficiency
- giving constant current at start
- smooth control without dissipating energy.

disadvantages:

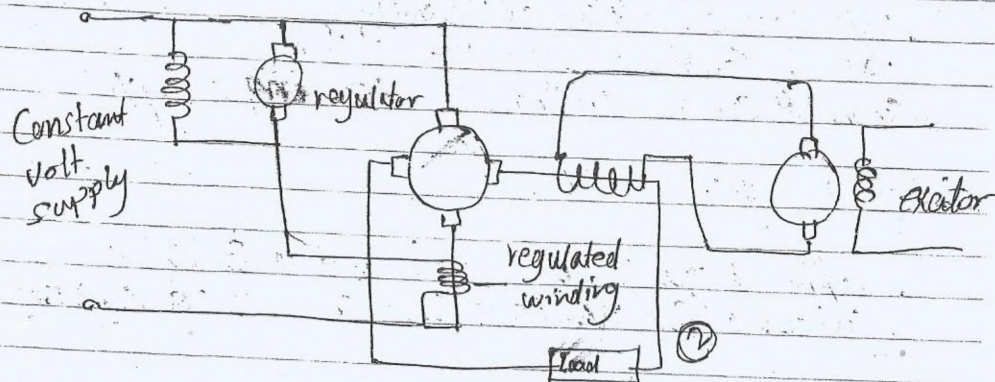
- after beginning we can't reduce I_2 to be suitable for various load. so we used variator wd



fig(c)



* The Complete metadyne set:-



* Variator winding:-

- its a winding feed from dc exciter wound round the pole and produce of flux with or opposite that produced by I_2 so we can control I_2

- this variator winding destroys the transformer property of the metadyne where.

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$E_1 = k I_2 + k_v I_v$ (not transformer property)

when $I_v = 0 \Rightarrow E_1 = k I_2$ (transformer property)

+ve Variator excitation when flux produced is in same direction that produced by I_2

(-ve) variator exciter when flux produced opposite direction of I_2 flux.

* regulator winding:-

- used to maintain metadyne it's transformer property - it produce a flux this flux effect the output current and power output.

- if this regulator current is adjusted correctly the output power remains constant to input power

$$E_2 = k I_1 + k_r I_r$$

$I_r, I_v \rightarrow$ Variator, regulator current

$k_v, k_r \rightarrow$ constant of M/C

$$P_i = E_1 I_1 = k I_1 I_2 + k_v I_1 I_v$$

$$P_o = E_2 I_2 = k I_1 I_2 + k_v I_2 I_r$$



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to maintain transformer property we have

$$P_i = P_o$$

$$E_1 I_1 = E_2 I_2 \Rightarrow K V I_1 I_V = K_r I_2 I_r$$

Ex 250 ton, mainline service $V_{avg} = 32 \text{ MVA}$

$$S = 1.25, a = 1.25, b = 2.5 \text{ M.p.h. } 8-5$$

trap/Bridal, $E.C \text{ kWhr}$, $r=12$, $\eta_{motor} = 80\%$

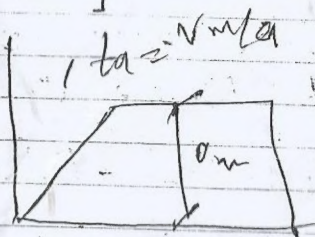
$W_e = 110 \text{ ton}$, no free rain,

Energy consumption = ??

$$\delta E.C = 0.028 \frac{W_e \cdot V_m^2}{W \cdot S} + 2 \frac{S'}{S} [r \pm 22 \sqrt{4Gi}]$$

$$(E.C) = \left[0.028 \frac{W_e}{W} \frac{V_m^2}{S} + 2 r \frac{S'}{S} \right] \times W S$$

$$S' = \frac{1}{2} \tan V_m$$



$$V_m = \frac{1}{2} K [T - \sqrt{T^2 - 14400 S K}]$$

$$K = \frac{1}{2a} + \frac{1}{2b}, T = \frac{S}{N} = \frac{1.25}{32/3600} = 50$$

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$$E.C = \frac{E.C}{\eta_{motor}}$$

